

# Examining Wireless Power Transfer

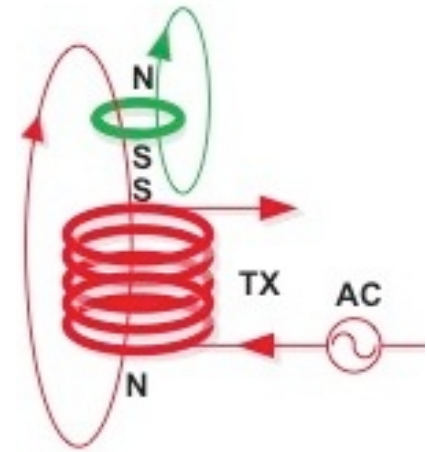
John Rice

# Agenda

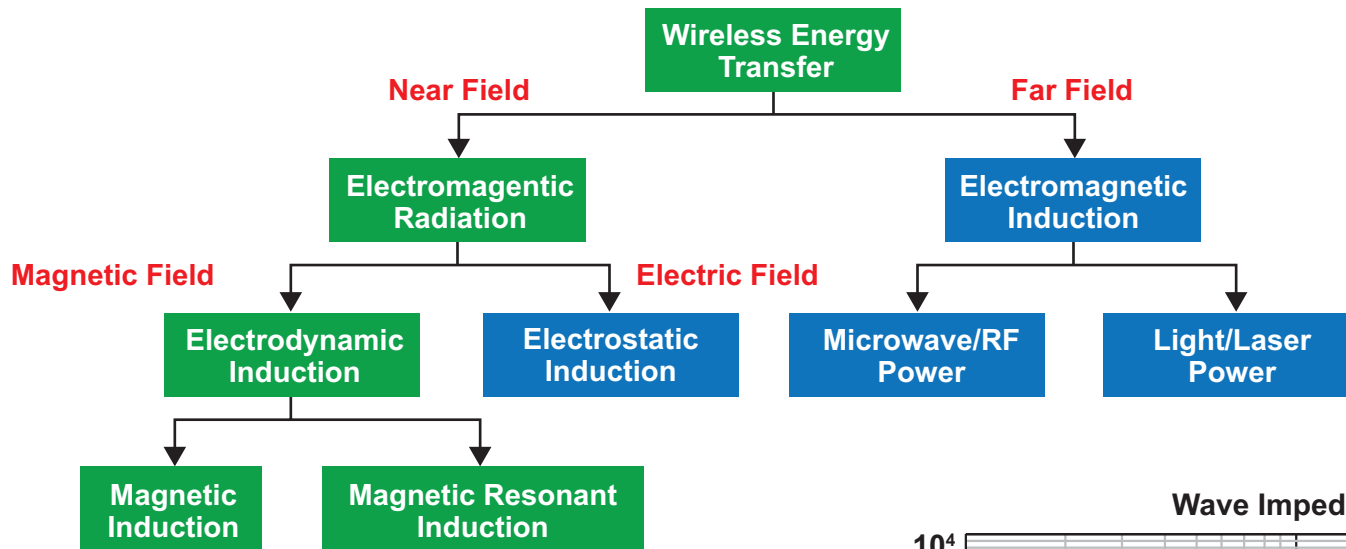
- **Introduction** **5 min.**
  - Foundational principles of electromagnetics
  - Power transfer - near and far field
- **Existing and Emerging Wireless Power Standards** **5 min.**
  - WPC, PMA, A4WP comparison
  - Electromagnetic field safety implications of WPT
- **Theory of Operation** **20 min.**
  - Considering loosely coupled coils
  - Modeling resonant power transfer
  - Magnetic link efficiency
  - Topological analysis with SPICE and FEA
- **Design Considerations** **20 min.**
  - RX to TX communication
  - Intelligent voltage positioning and load response
  - EMI, efficiency/loss measurement
  - Foreign object detection – eddy loss detection
  - Single coil, 5 W WPC design example

# Notable Dates in Wireless Power Transfer

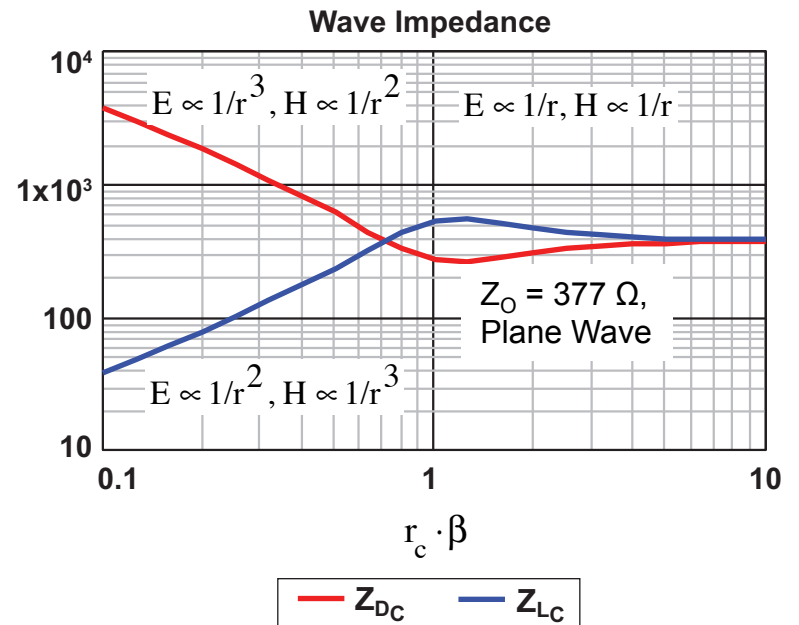
- **1820:** **Biot–Savart / André-Marie Ampère / H. Oersted** discover and quantify relationship between electric current and magnetic fields
- **1831:** **Michael Faraday / H. Hertz** discover electromagnetic induction
- **1834:** **Lenz** (Lenz's law) → **N. Callan** invents the electrical transformer
- **1864:** **James Clerk Maxwell** synthesizes previous observations and mathematically models electromagnetic radiation
- **1891-1917:** **Nicola Tesla** – enormous contribution to the practical application of resonant power transfer and electromagnetic induction; numerous discoveries and patents
- **2007:** WiTricity research group, led by **Professor Marin Soljacic** advances magnetic resonance to wirelessly power a 60 W light bulb with 40% efficiency at 2 m using 60 cm-diameter coils
- **2008/9:** A consortium of companies called the **Wireless Power Consortium (WPC)** announces the evolution of a industry standard for low-power (5 W) inductive charging



# Electromagnetic Wave Propagation



- Field defined by antenna and distance from source
- Dipole(red) and loop(blue) antennas shown
- Wave impedance = E/H, converges at  $\lambda \gg 1$
- Reactive near field below  $\lambda/2\pi$  is non-radiative

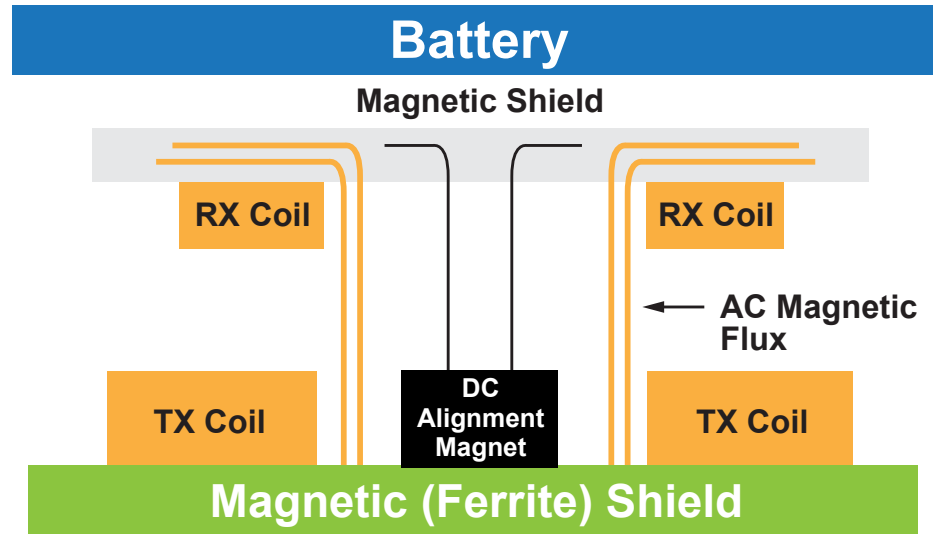


# Race for a Wireless Charging Standard

Safety, Performance, Reliability and Interoperability



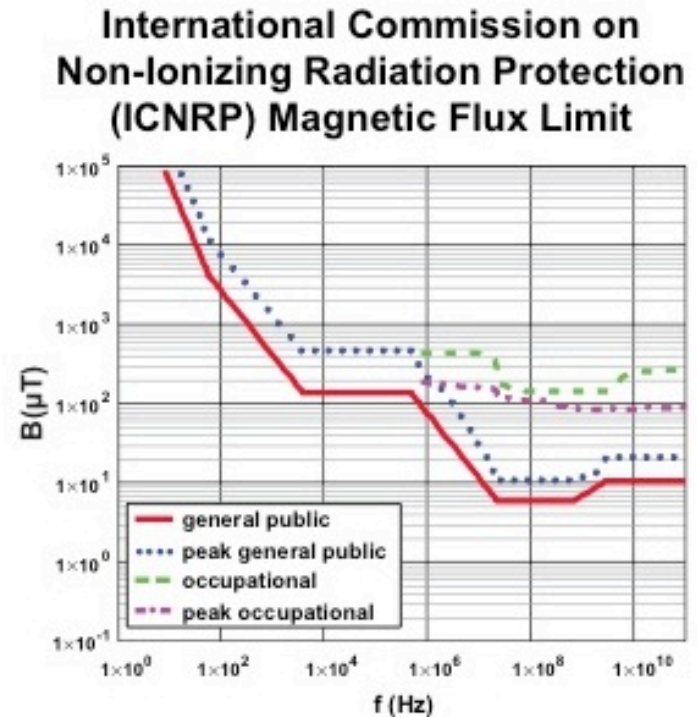
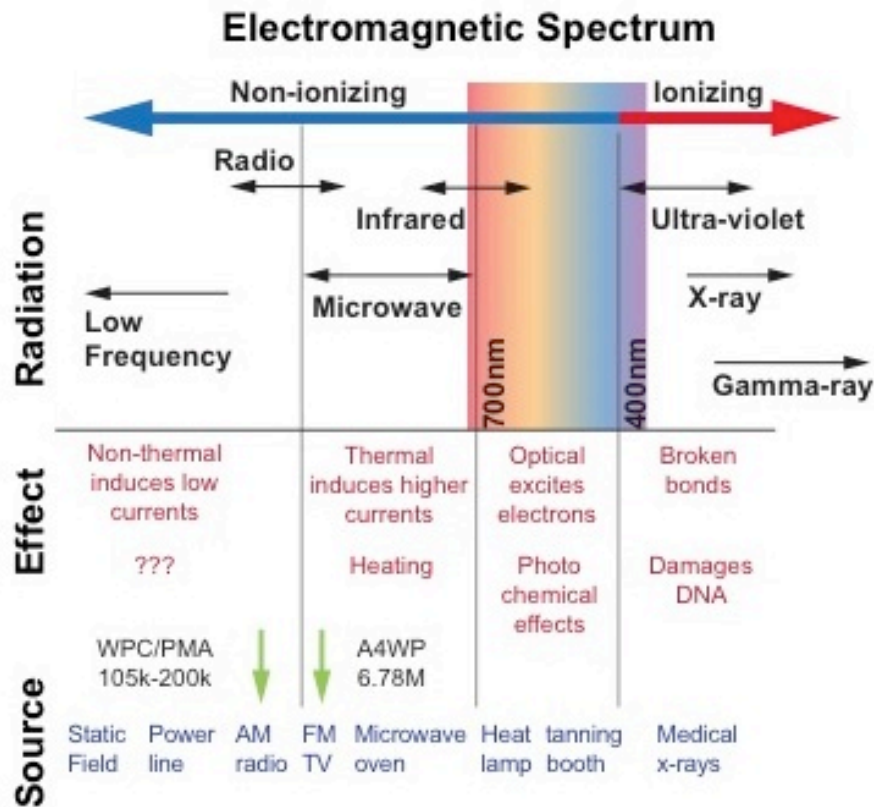
Alliance for Wireless Power



Protocols	Power Frequency Band	Communication Frequency Band	Range of Coupling
Wireless Power Consortium (WPC)	105-205 kHz	Same as power transfer band	0.4 to 0.7
Powermat (PMA)	277-357 kHz	Same as power transfer band	0.6 to 0.8
Alliance for Wireless Power (A4WP)	6.78 MHz	2.4GHz ISM (ZigBee or BLE)	0.1 to 0.5

# Safety Considerations

## Electromagnetic Radiation Effect



Frequency Range	E-field (V/m)	H-field (A/m)	B-field ( $\mu\text{T}$ )
0.025-0.8 kHz	250/f	4/f	5000/f
0.15-1 MHz	87	0.73/f	0.92/f
1-10 MHz	87/f <sup>0.5</sup>	0.73/f	0.92/f

# Theory of Operation

$$\oint \mathbf{E} \cdot d\mathbf{A} = \frac{\Sigma Q}{\epsilon_0}$$

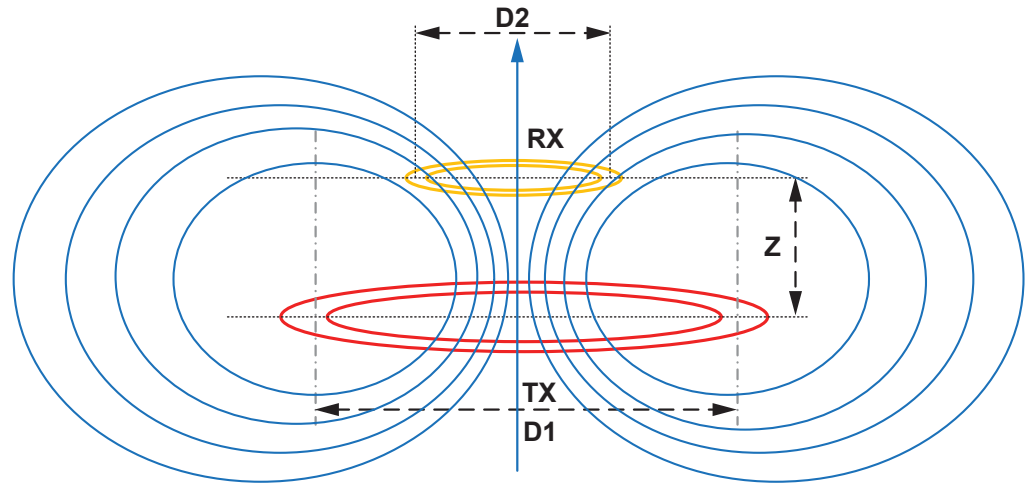
$$\oint \mathbf{B} \cdot d\mathbf{A} = 0$$

$$\oint \mathbf{E} \cdot d\mathbf{l} = -\frac{d}{dt} \oint \mathbf{B} \cdot d\mathbf{A}$$

$$\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_{enc} + \mu_0 \epsilon_0 \frac{d\phi_E}{dt}$$

$\mu_0$  = Vacuum \_ permeability

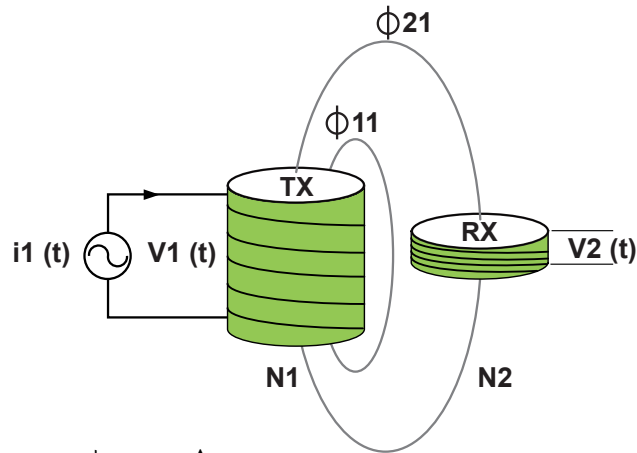
$\epsilon_0$  = Vacuum \_ permittivity



# Loosely Coupled Coils

## Self and Mutual Inductance

Physical representation of flux coupling



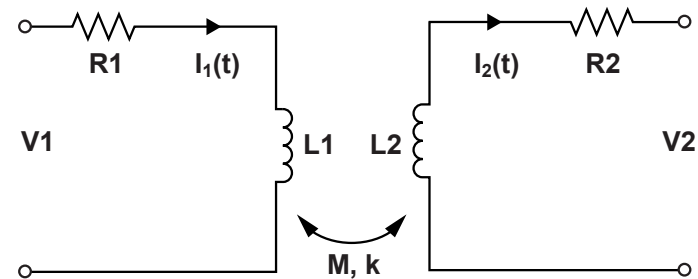
$$P = \frac{\phi}{Ni} = \frac{\mu A}{l}, \phi = PNi$$

$$V_c = N \frac{d\phi}{dt} = N \frac{d(PNi)}{dt} = N^2 \frac{\mu A}{l} \frac{di}{dt} = L \frac{di}{dt}$$

$$L = \frac{N\phi}{i}, \phi_1 = \phi_{11} + \phi_{21}$$

$$V_2 = N_2 N_1 P_{21} \frac{di_1}{dt} \rightarrow M = N_2 N_1 P_{21}$$

Electrical representation of flux coupling



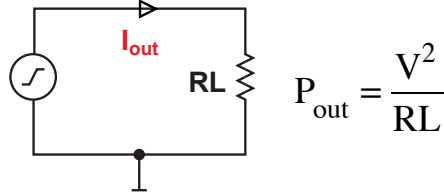
$$V_1(t) = R_1 i_1(t) + L_1 \frac{di_1(t)}{dt} + / - M \frac{di_2(t)}{dt}$$

$$V_2(t) = R_2 i_2(t) + L_2 \frac{di_2(t)}{dt} + / - M \frac{di_1(t)}{dt}$$

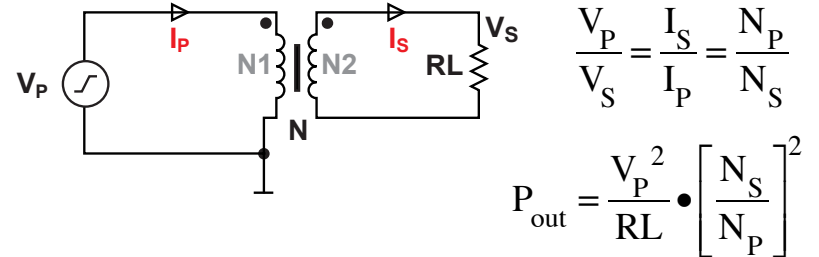


# Power Transfer, Wired and Wireless

Wired/  
Tightly  
Coupled

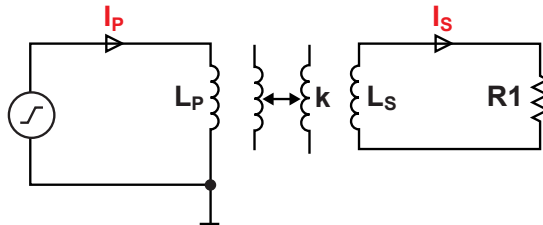


**Ideal Transformer  $k = 1$**

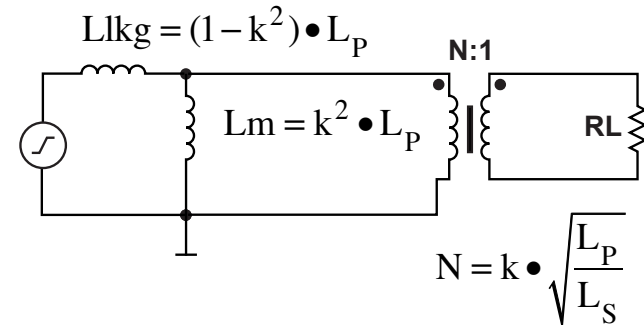


**Non-Ideal Transformer  $k \ll 1$**

Loosely  
Coupled  
WPT

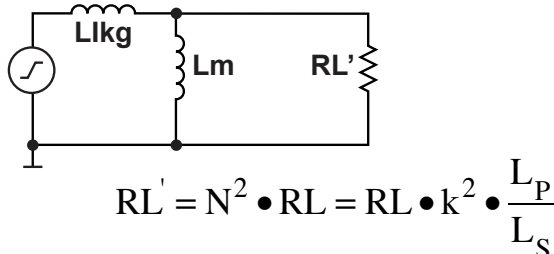


**Cantilever Transformer Model**

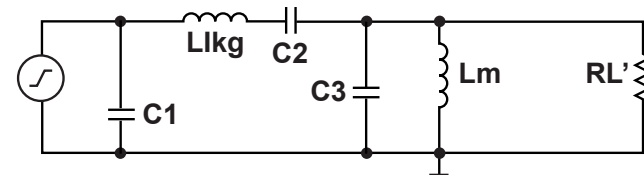


**Load Reflected to Primary  
is Proportional to  $k^2$**

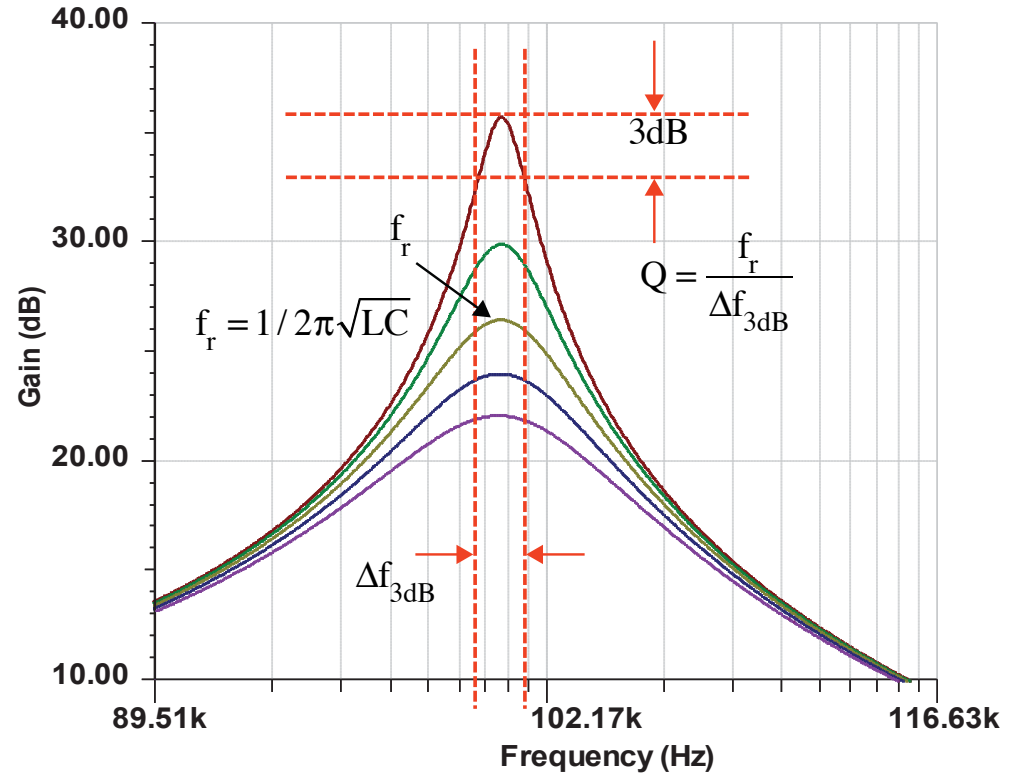
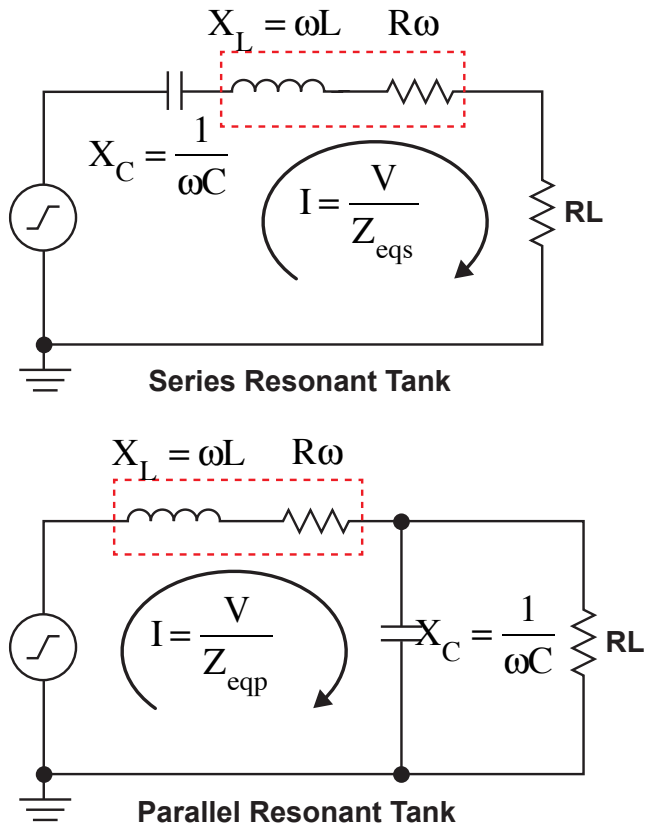
Load  
Reflected  
to Primary



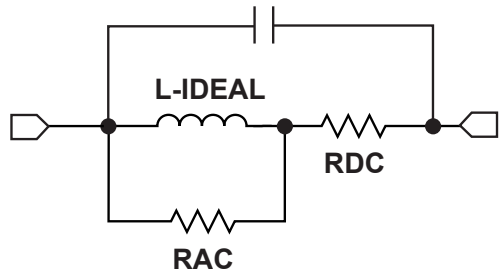
**Leakage Impedance Cancelation**



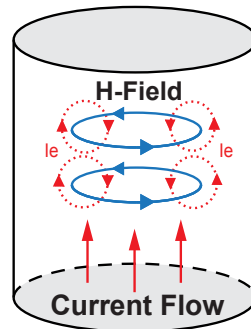
# Considering Resonance



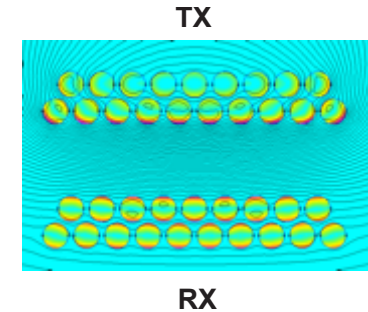
# Coil Skin and Proximity Losses (Eddy Induced Losses)



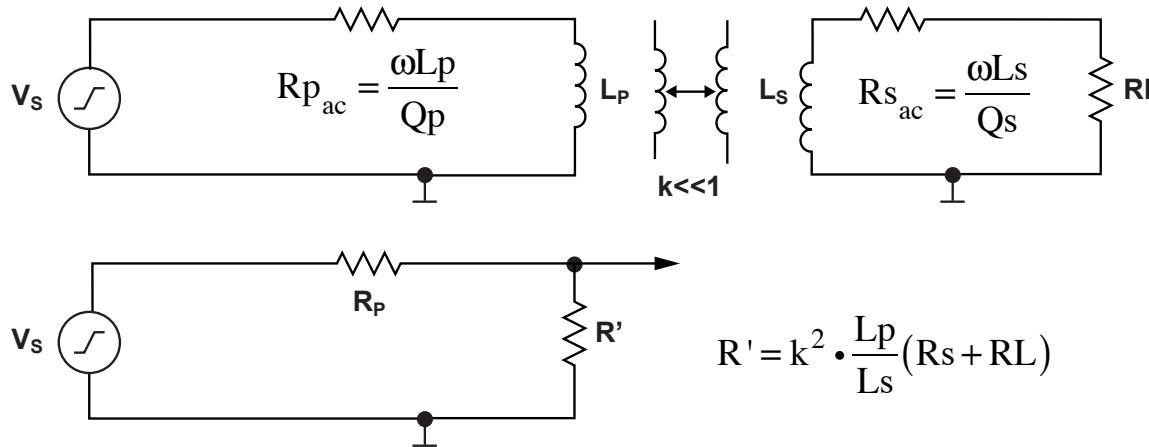
Non-Ideal TX/RX Inductor



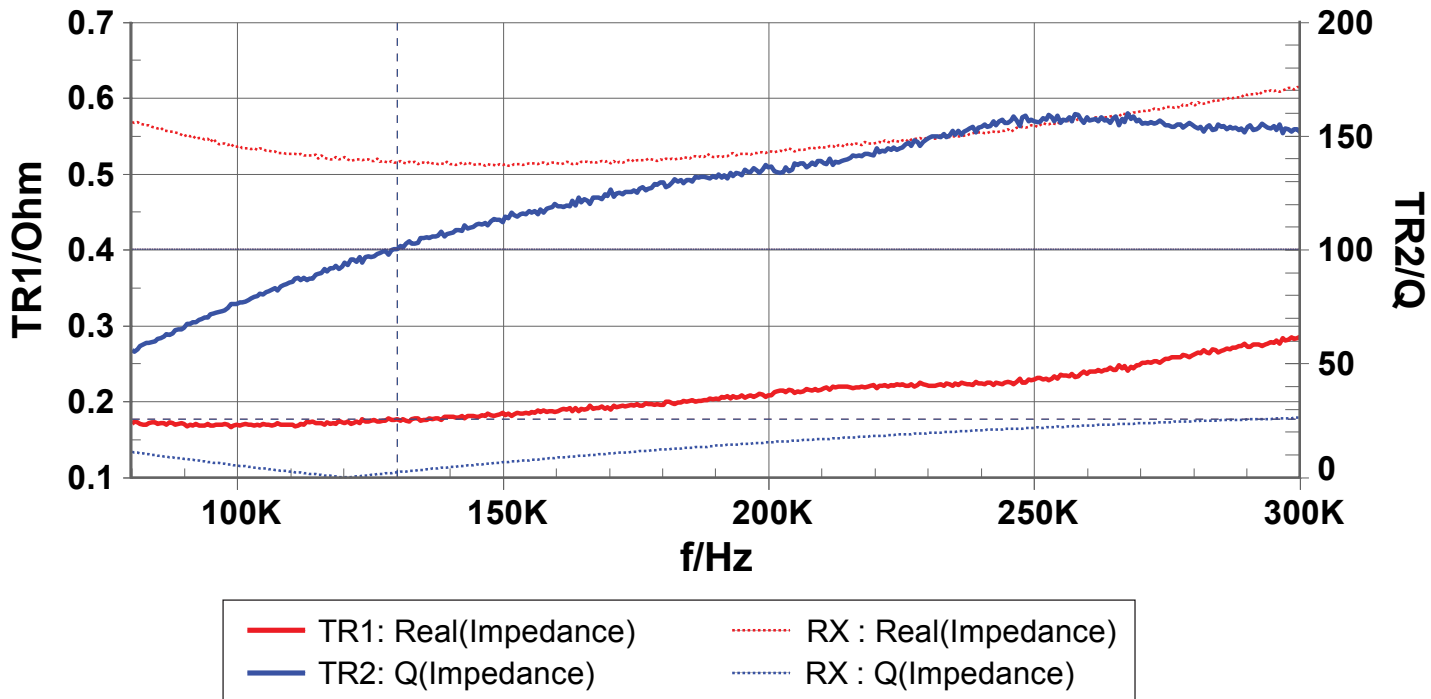
Skin Effect



Proximity Effect



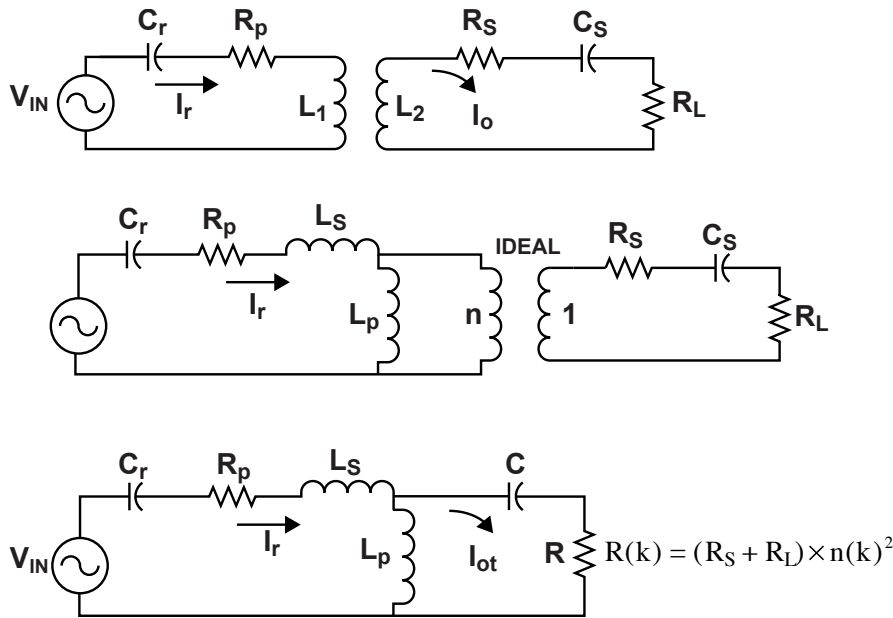
# Typical WPC TX/RX Coil Q and Skin/Proximity Effect



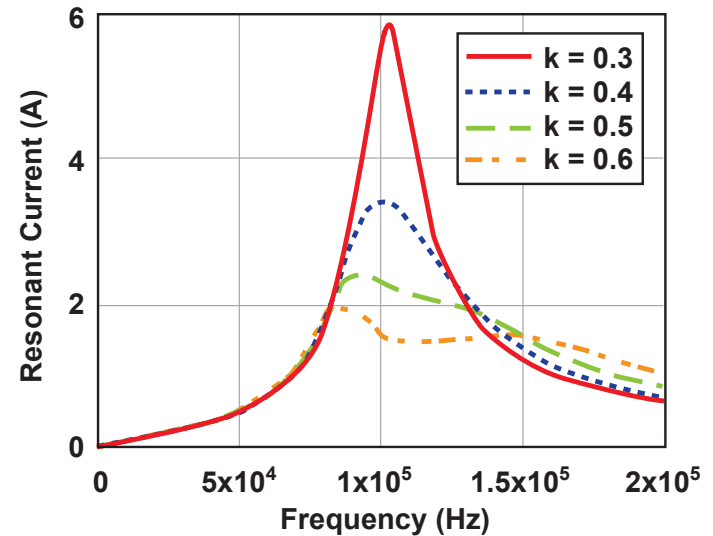
**TX:**  
 43 mm diameter with shield  
 Litz wire, 105 strand  
 20 turns, 2 layers  
 $Q = 100 @ 130 \text{ kHz}$   
 $R_{ac} = 176 \text{ m}\Omega$

**RX:**  
 40 x 30 mm with shield  
 Litz wire, 2 strands  
 14 turns, 1 layer  
 $Q = 2.3 @ 130 \text{ kHz}$   
 $R_{ac} = 515 \text{ m}\Omega @ 130 \text{ kHz}$

# Primary Current vs. Frequency and Coupling Coefficient



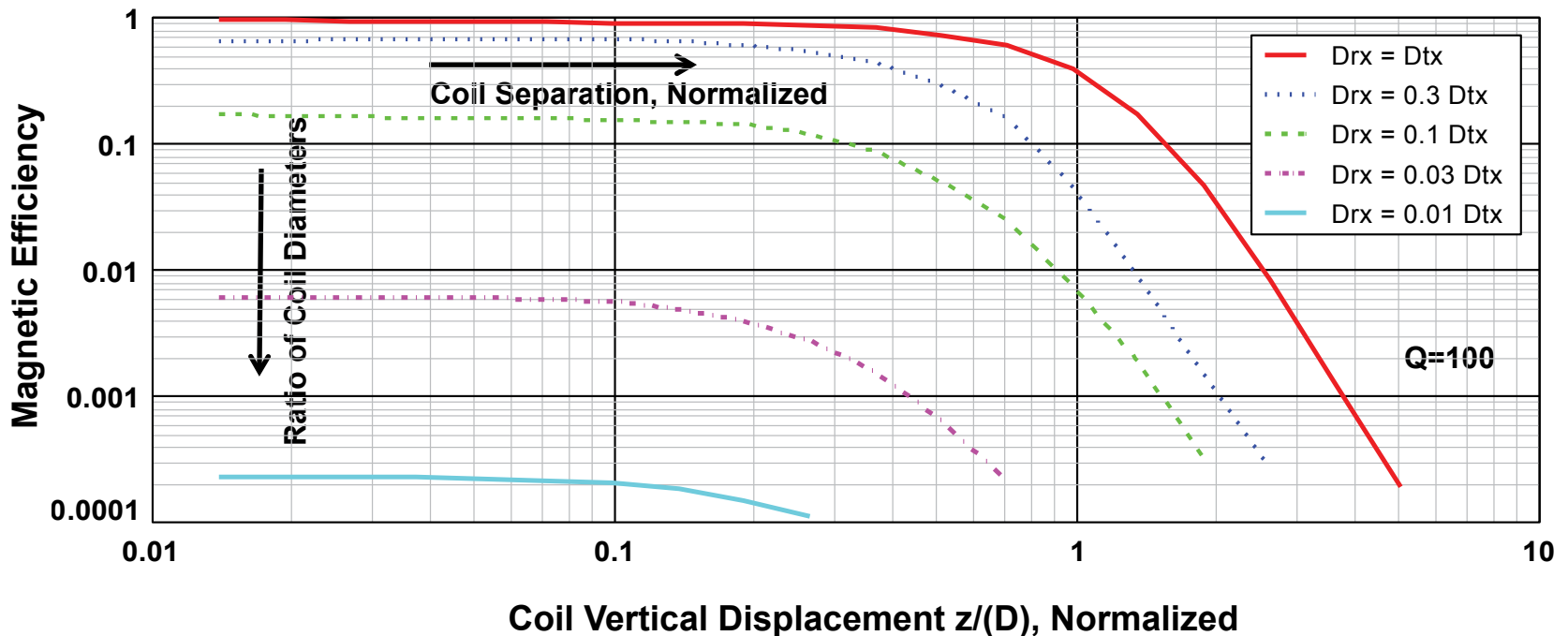
$$i_r(f, k) = \frac{V_{\text{fundamental}}}{Z_{\text{IN}}(f, k)}$$



$$Z_{\text{IN}}(f, k) = R_p + R(k) \cdot \frac{Q_p(f, k)^2}{1 + Q_p(f, k)^2} + j(XL_s(f, k) - XC_r(f)) + R(k) \cdot \frac{Q_p(f, k)}{1 + Q_p(f, k)^2}$$

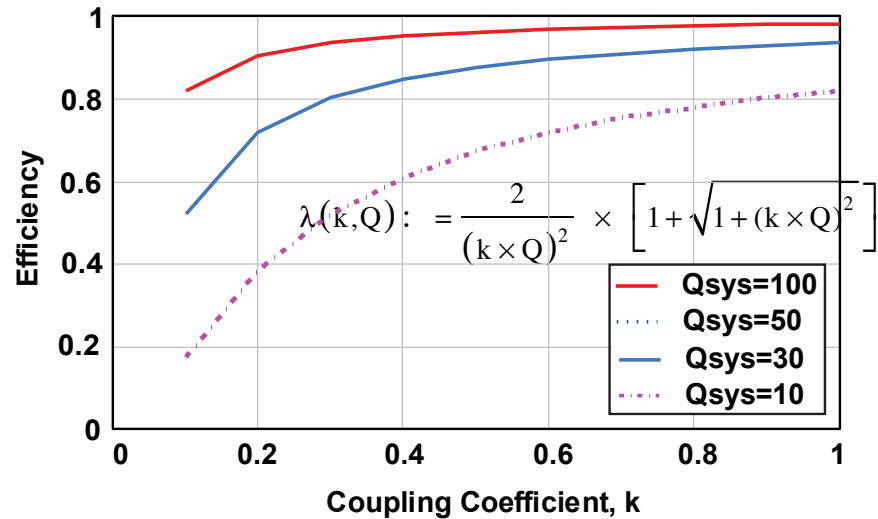
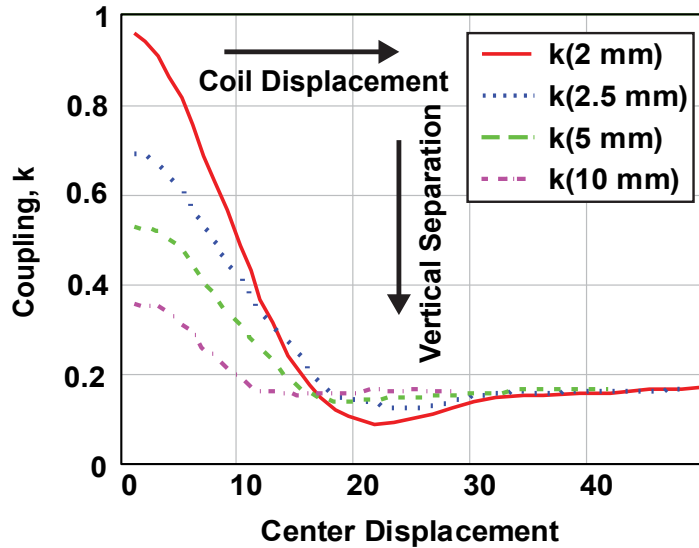
# Coupling Efficiency

Coupling Efficiency in Relationship to Coil Separation ( $z$ ) and the Ratio of Coil Diameters



# Magnetic Figure of Merit $F(k, Q)$

## 30 mm Planar Coils



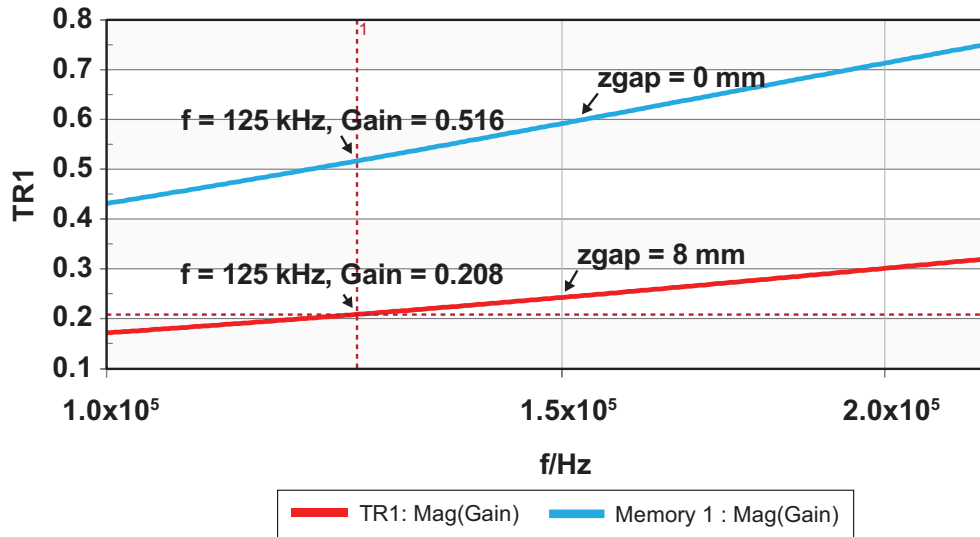
- $Q$  = geometric mean of coil quality factors =  $\sqrt{Q_p \times Q_s}$
- $Q$  influenced strongly by skin and proximity effect

- High  $Q$  compensates for poor coupling
- High  $Q$  requires greater control bandwidth

# Coupling Coefficient and Mutual Inductance from Transfer Gain

$$k = \sqrt{\frac{L_{rx}}{L_{tx}}} \cdot \frac{V_{tx}}{V_{rx}} = \frac{\text{Gain}}{\sqrt{\frac{L_{rx}}{L_{tx}}}} \quad \begin{array}{l} L_{rx} = 10.8 \mu\text{H} \\ L_{tx} = 25 \mu\text{H} \end{array}$$

$$M = k \cdot \sqrt{L_{rx} \cdot L_{tx}}$$



Typical 5 W coils  
Connected to a VNA

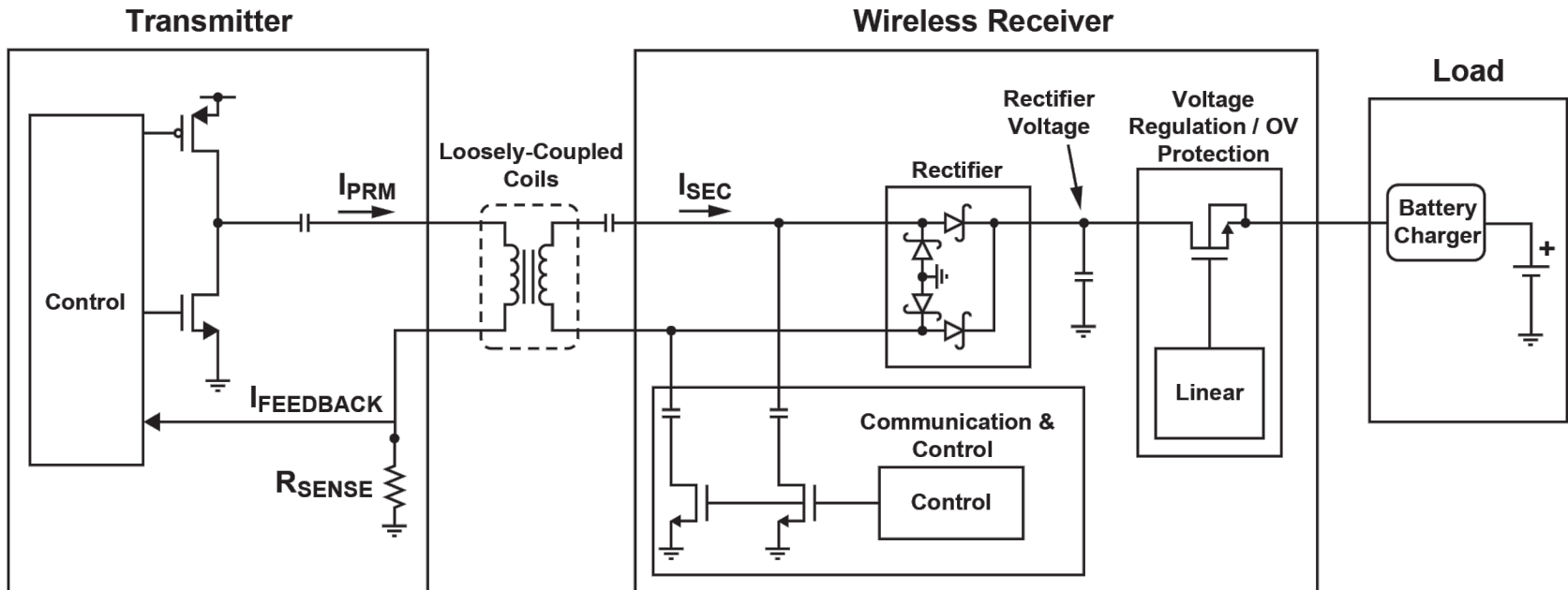
$$k(\text{gap} = 0 \text{ mm}) = \frac{0.516}{\sqrt{\frac{L_{rx}}{L_{tx}}}} = 0.83, \quad M = 13.6 \mu$$

$$k(\text{gap} = 8 \text{ mm}) = \frac{0.208}{\sqrt{\frac{L_{rx}}{L_{tx}}}} = 0.321, \quad M = 5.27 \mu$$



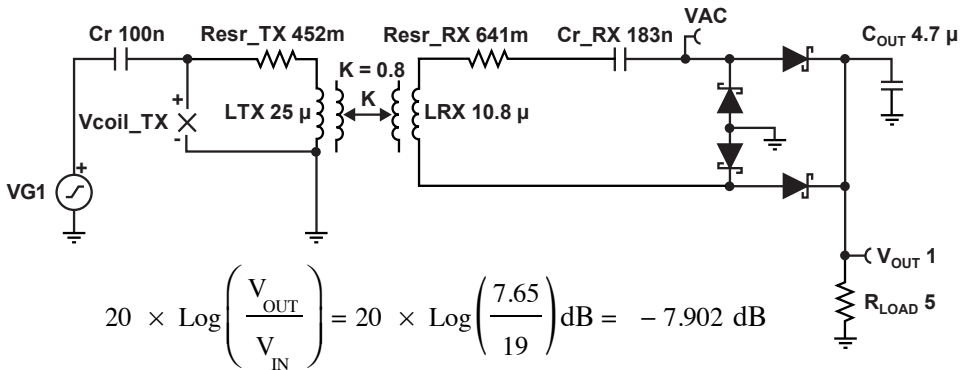
# Intelligent WPT

## Digital Power, Resonant Battery Charger

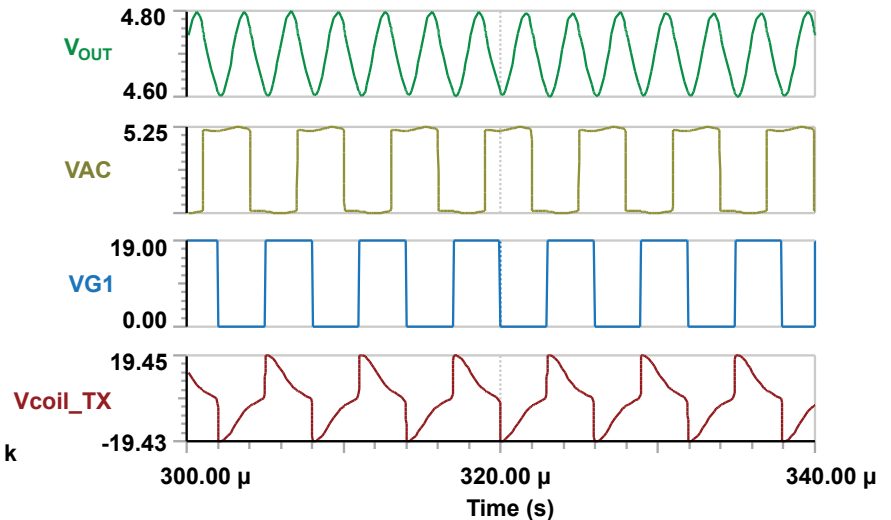
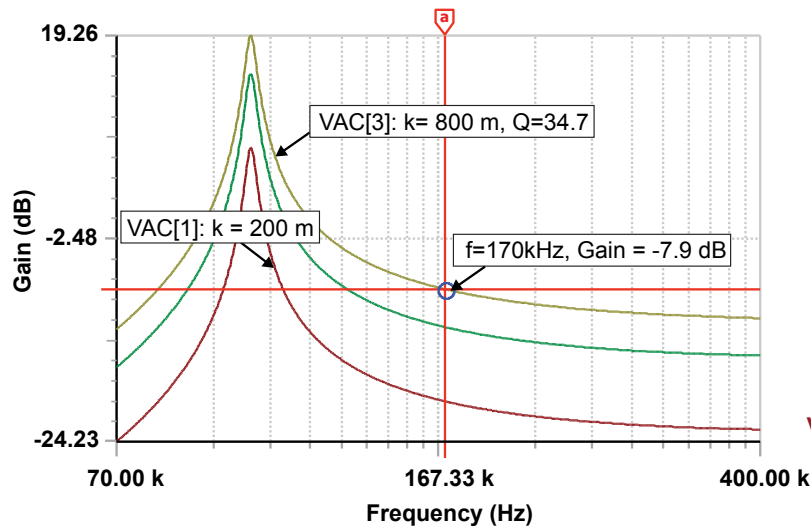


- A transmitter (TX) driving a resonant coupled inductor
- A receiver (RX) with rectification, load modulation and post regulation
- A load, commonly a single cell, secondary battery pack

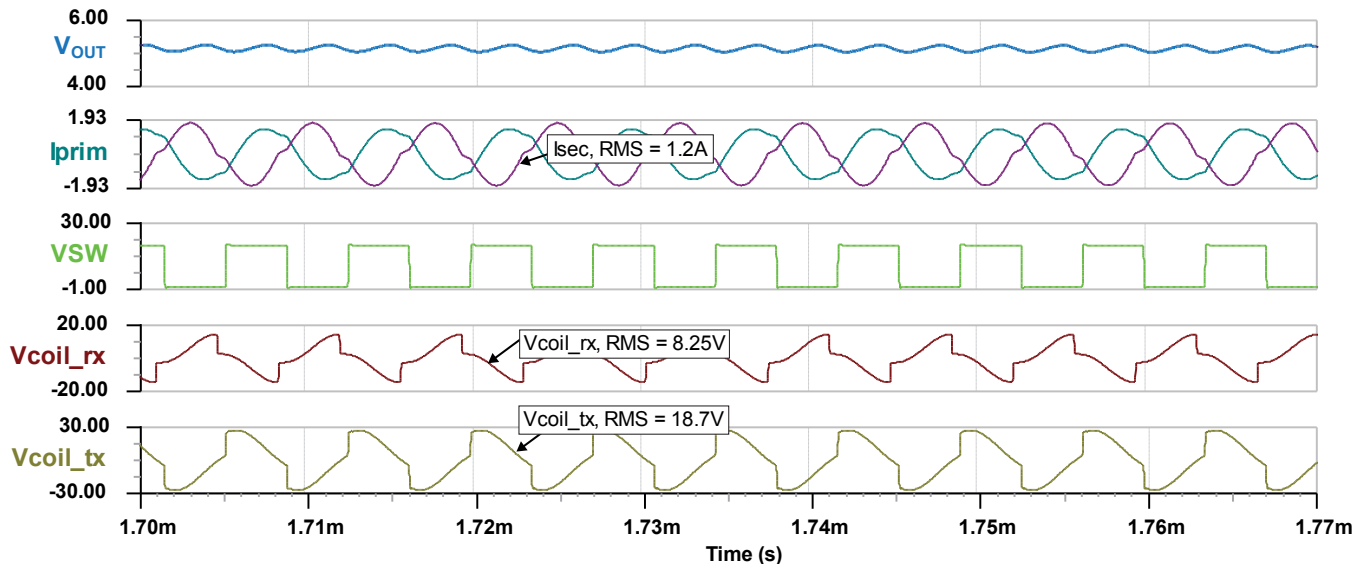
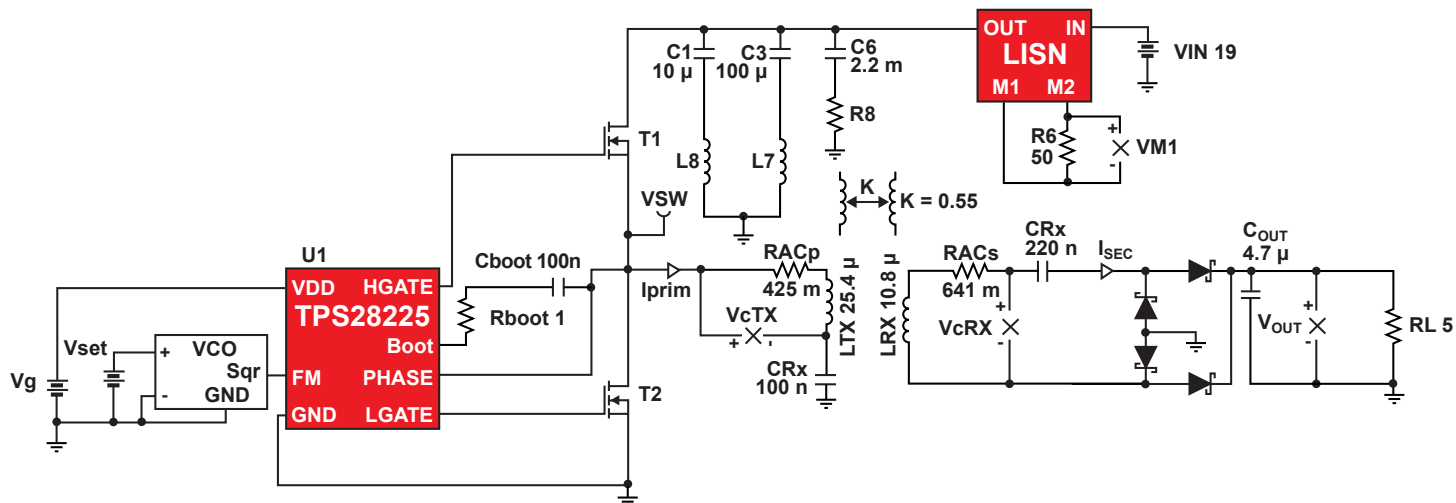
# Resonant Circuit Analysis



- VG1 is a variable frequency AC signal in frequency domain
- VG1 is a 50% duty cycle, 19 V square wave in the time domain
- Power regulated by changing the frequency or voltage

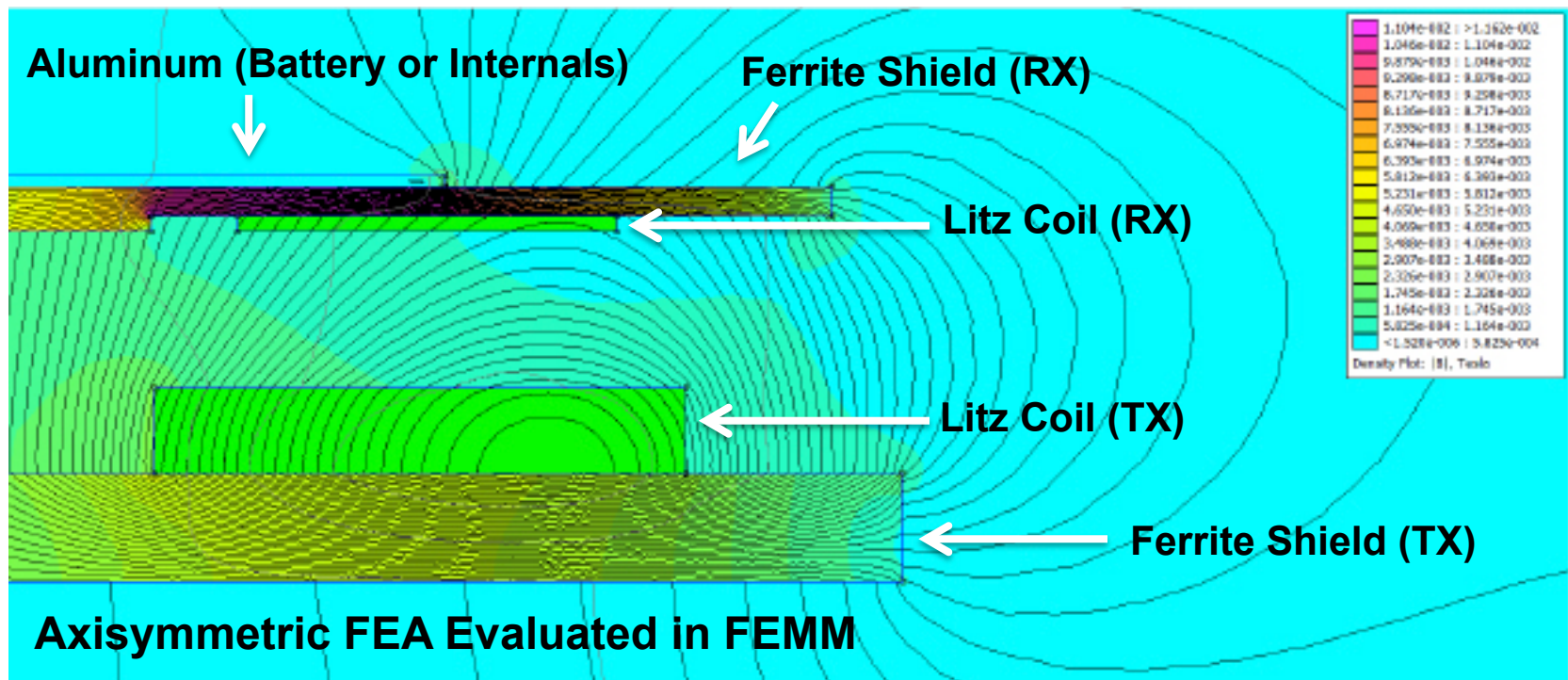


# Examining Circuit Behavior in SPICE



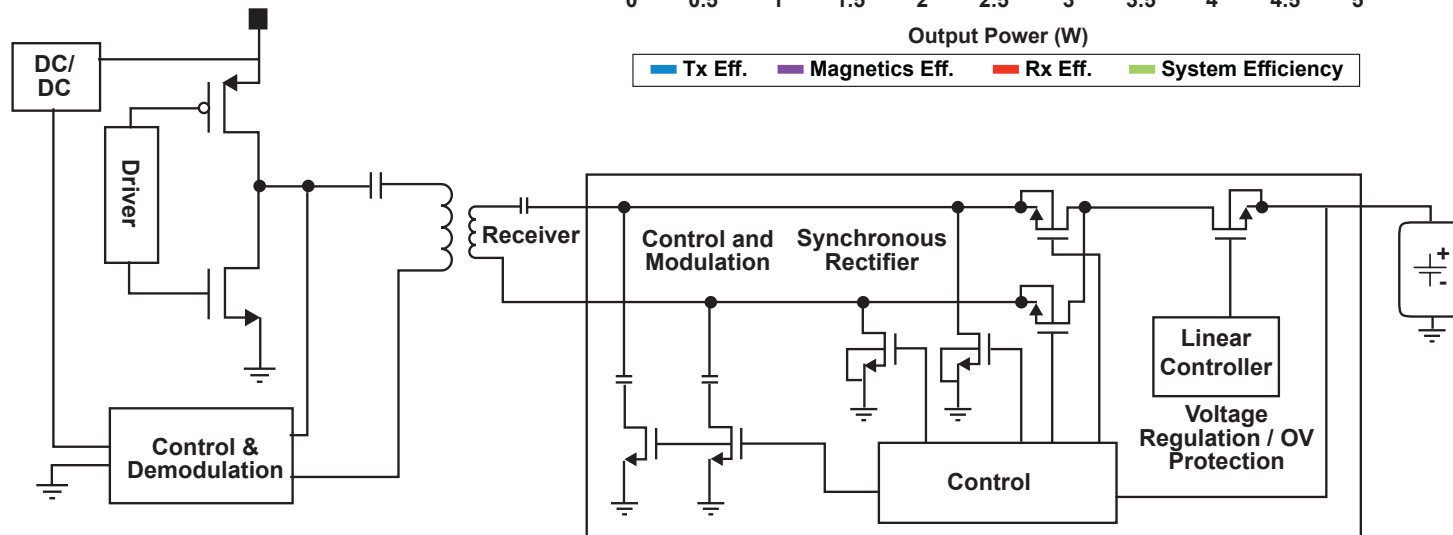
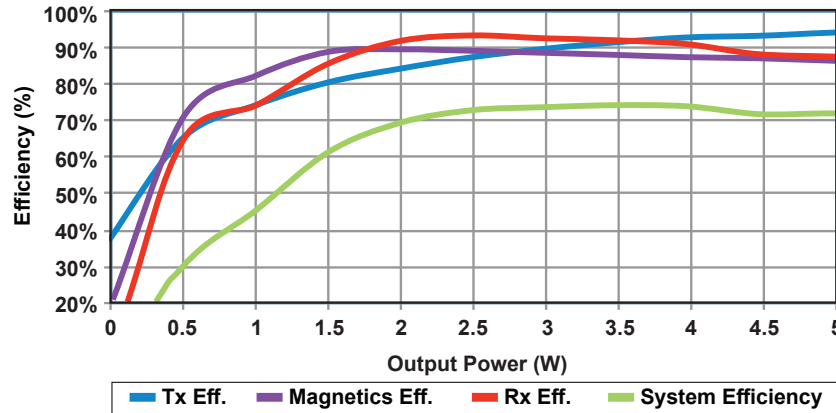
# 2-D FEA Plot of Magnetic Flux Between TX/RX Coils

- Receiver side shielding is important
- Poorly designed shields expose battery and external circuits to magnetic field
- AC/DC winding losses of TX/RX coils correspond with empirical results = 0.32 W



# Quantifying Losses – Typical 5 W Wireless Power Transmitter/Receiver

$$\eta = \frac{P_{OUT}}{P_{OUT} + P_{RX} + P_{TX}}$$

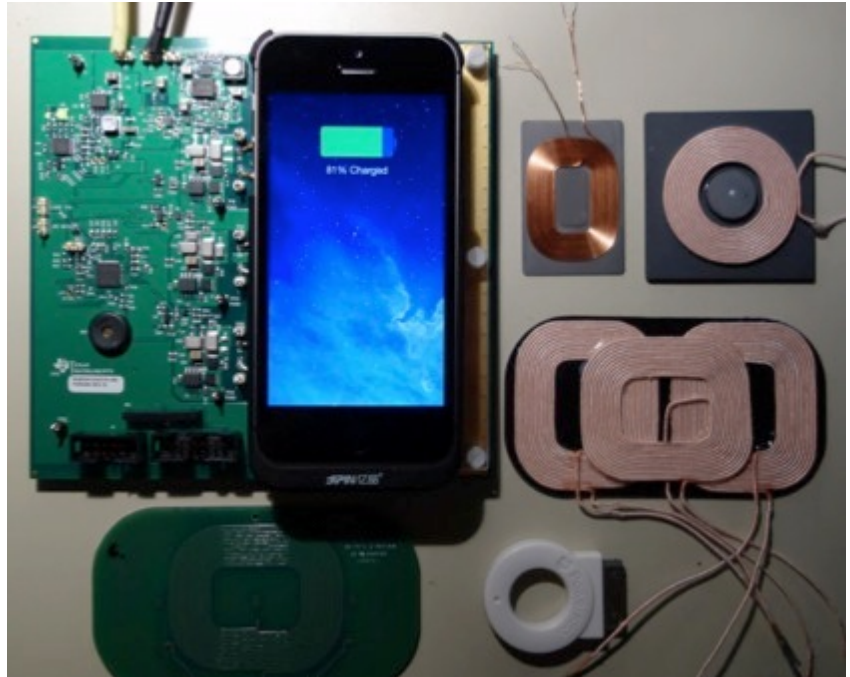


$$P_{TX} = P_{TXcoil} + P_{Bridge} + P_{control} + P_{DC-DC}$$

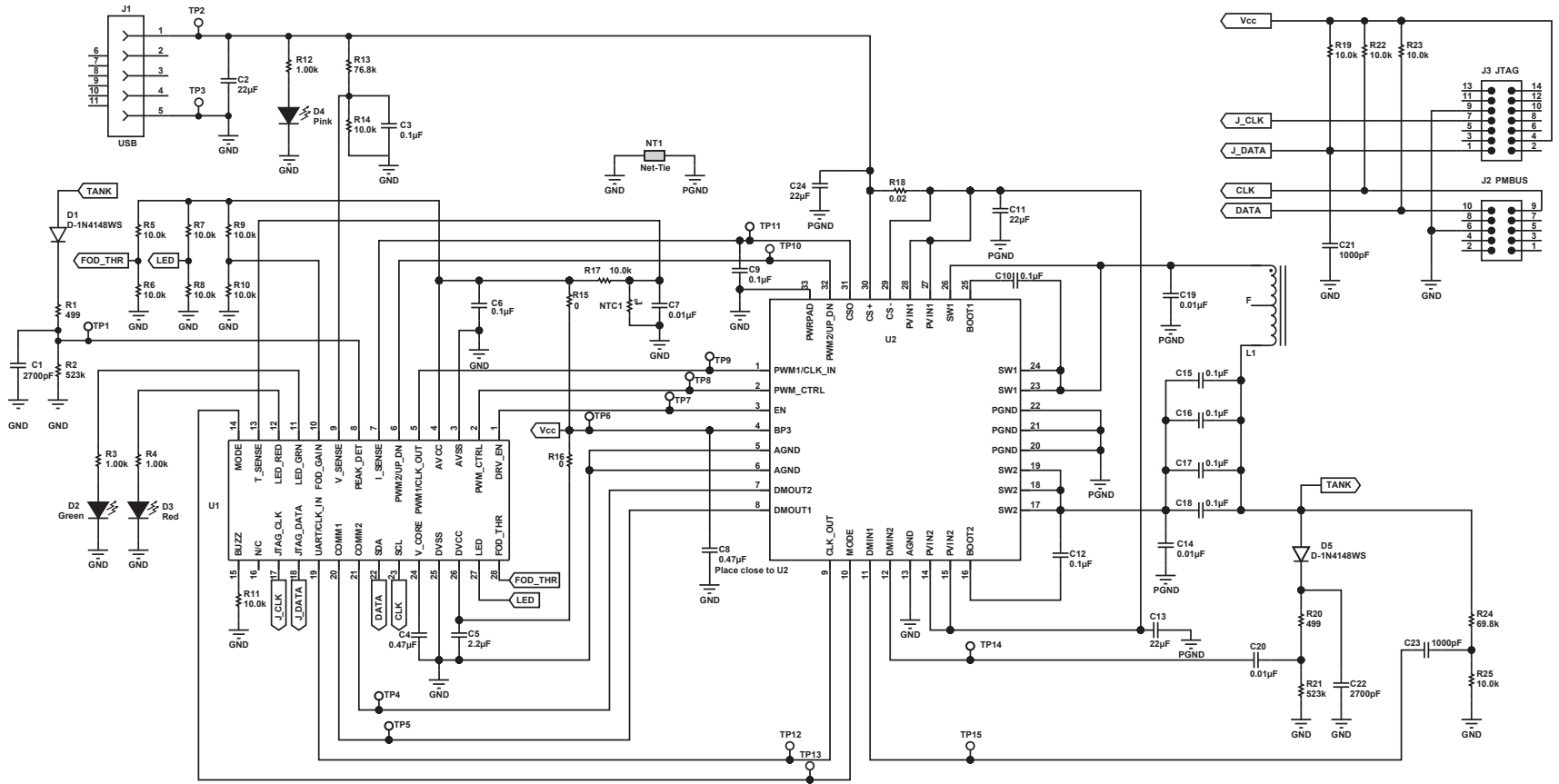
$$P_{RX} = P_{RXcoil} + P_{rectifier} + P_{Ido} + P_{comm}$$

# Design Considerations, WPC

- Feedback communication
- Loop response
- Foreign object detection
- Electromagnetic compatibility
- System efficiency

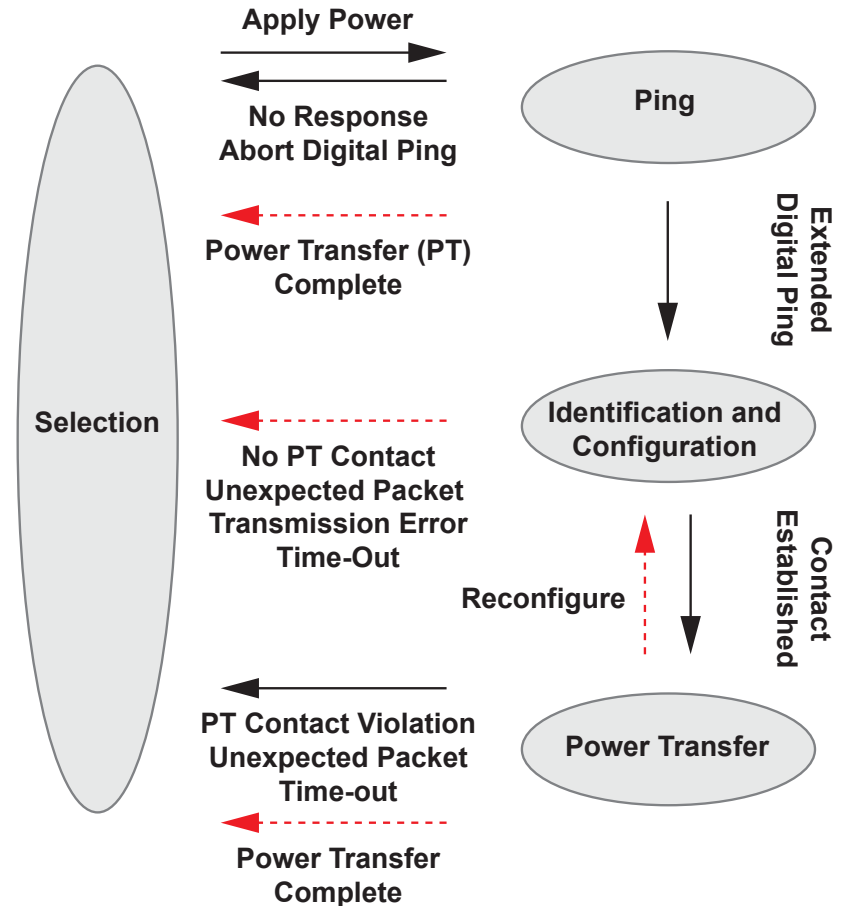


# WPC 1.1 Compliant 5 W TX Reference Design



# Qi Power Transfer Communication Protocol

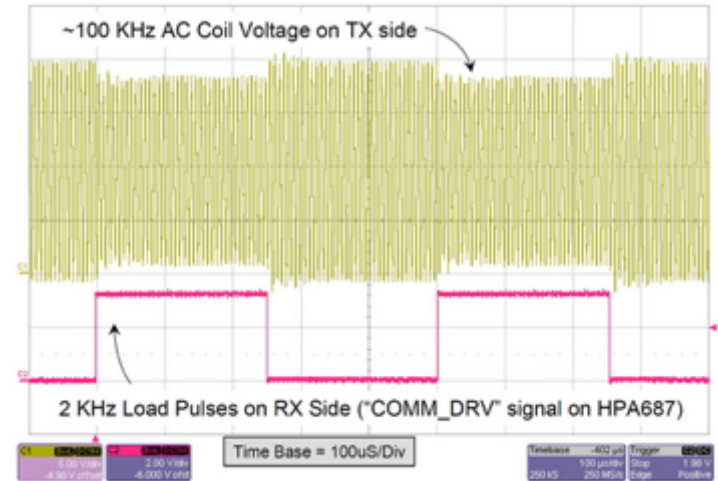
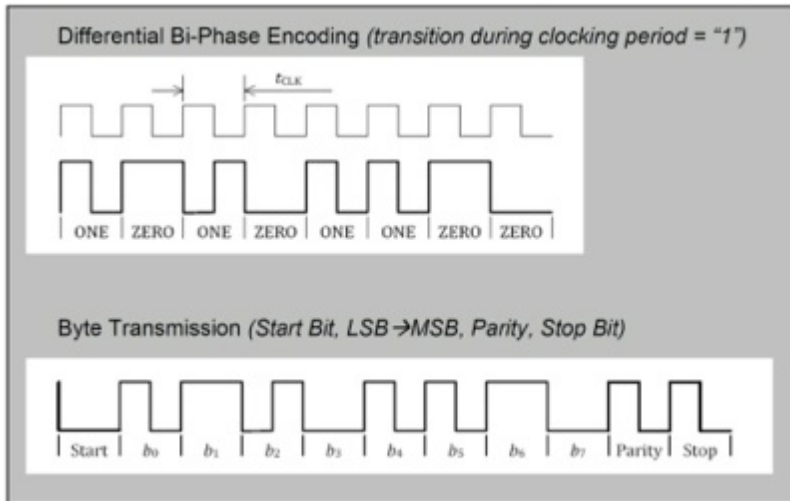
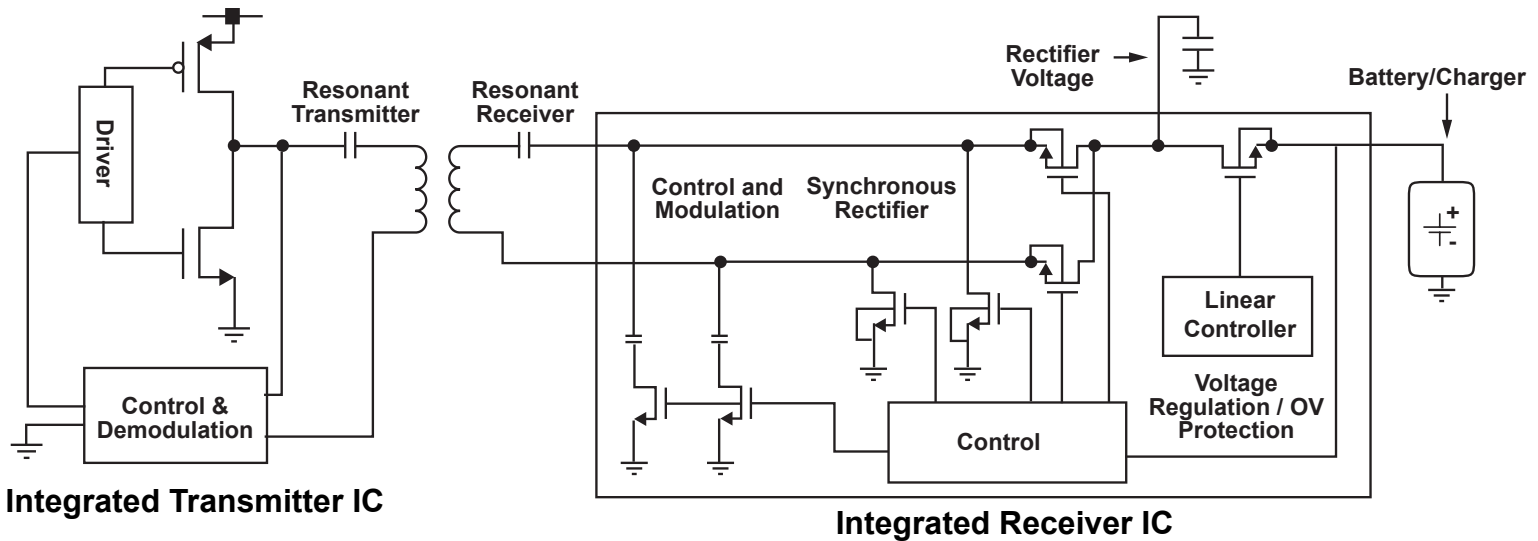
- **TX generates a shared magnetic field**
  - TX coil creates magnetic field
  - Magnetic field induces current in RX coil
- **Communication in power field**
  - TX waits until its field perturbed by RX
  - TX sends seek energy “ping”
  - TX waits for a digital response
  - If digital response is valid, transfer power
- **Power transferred at level needed**
  - RX reports power received/needed
  - TX adjusts power based on RX feedback
  - If feedback is lost, power transfer stops



From WPC Qi System Description. Part 1

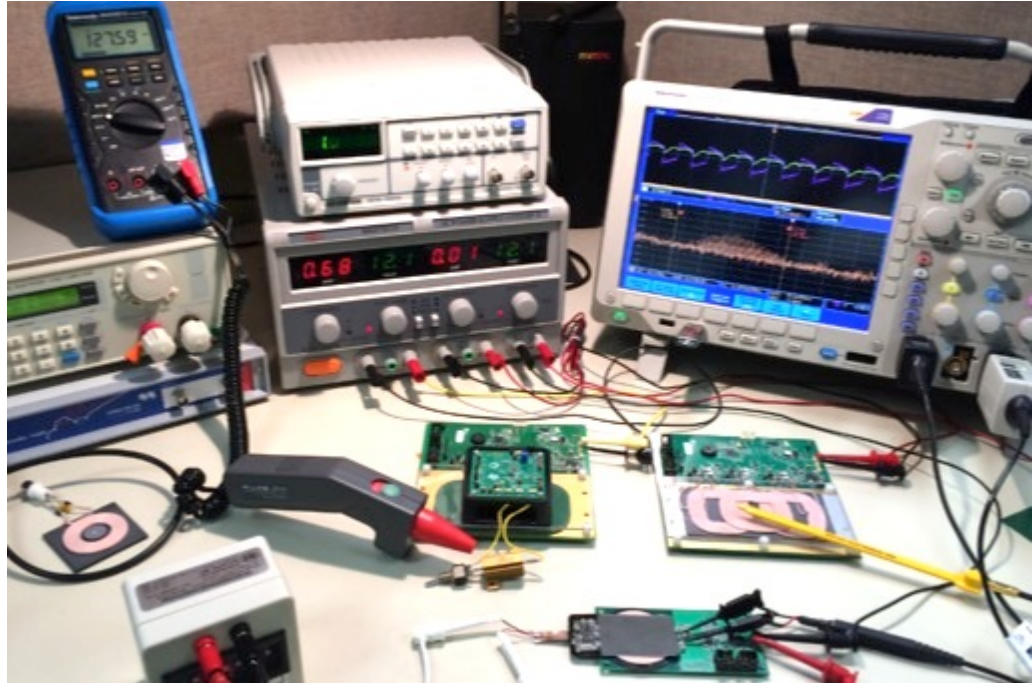


# WPC RX Load Modulation



# Measurement

- Power transfer waveforms
  - Coil resonance
  - Harmonic content
- Load response
- Efficiency –
  - Loss contributors
  - PCB coil vs. Litz
- RX/TX communication
- EMI, FOD
- Spatial freedom

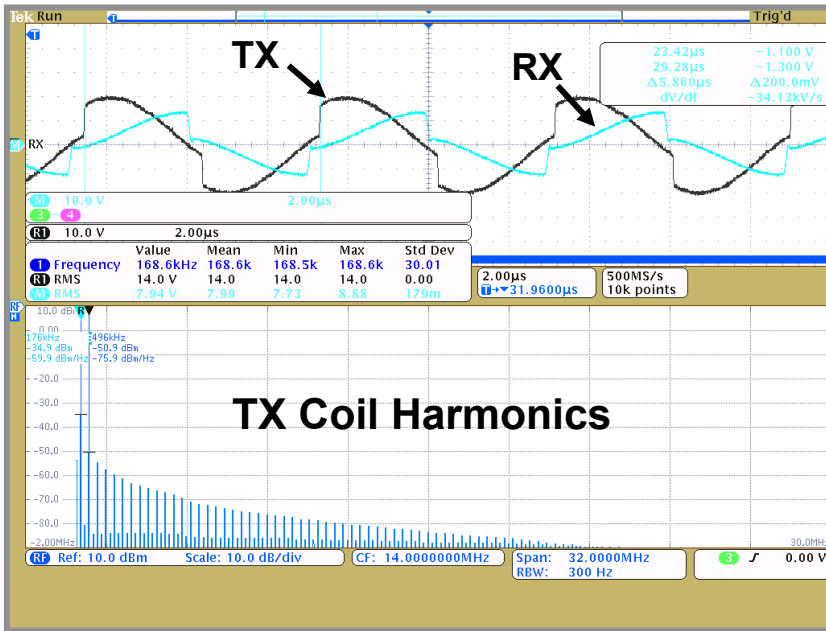


**VNA – Bode 100 – Coil gain/impedance characteristics**

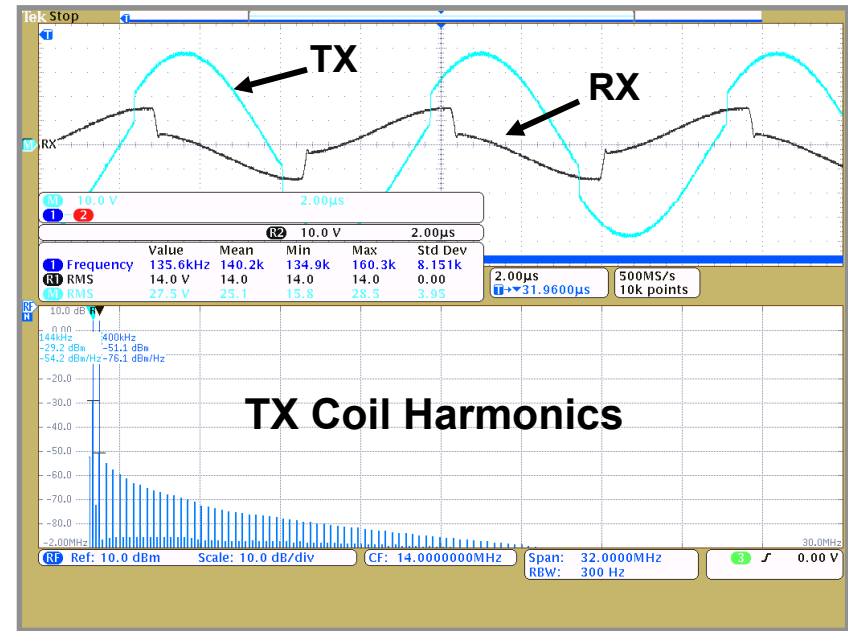
**MDO4104 – Mixed domain oscilloscope**

**Differential voltage probe capable of > 40 V, current probe, IR probe**

# Reference Design Waveforms at 5 W Time and Spectrum Domain

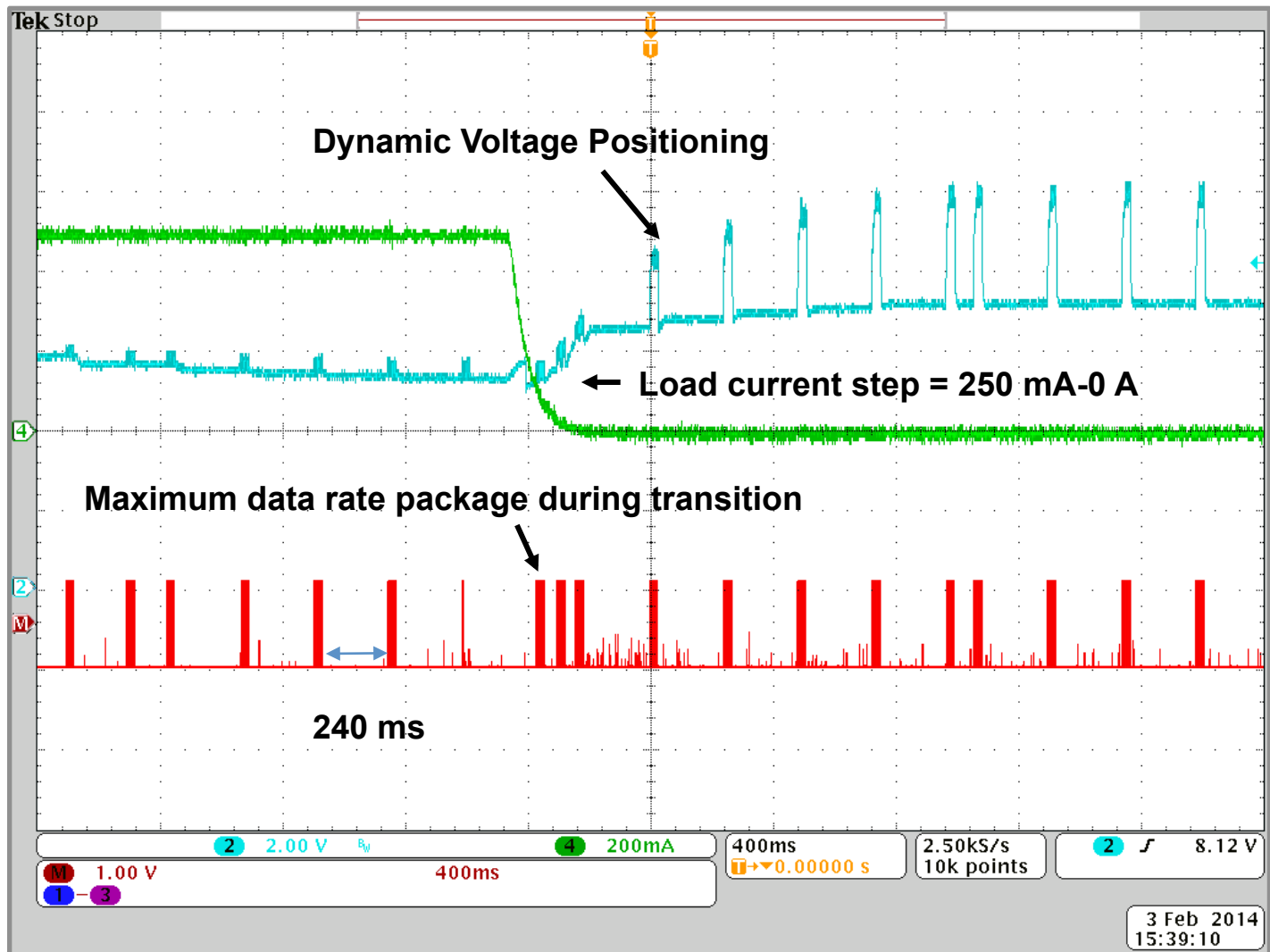


Centered coils force operation  
further from resonance  
 $V_{pp\_tx} = 20 \text{ V}$ ,  $f_{SW} = 170 \text{ kHz}$   
RMS gain = 0.56



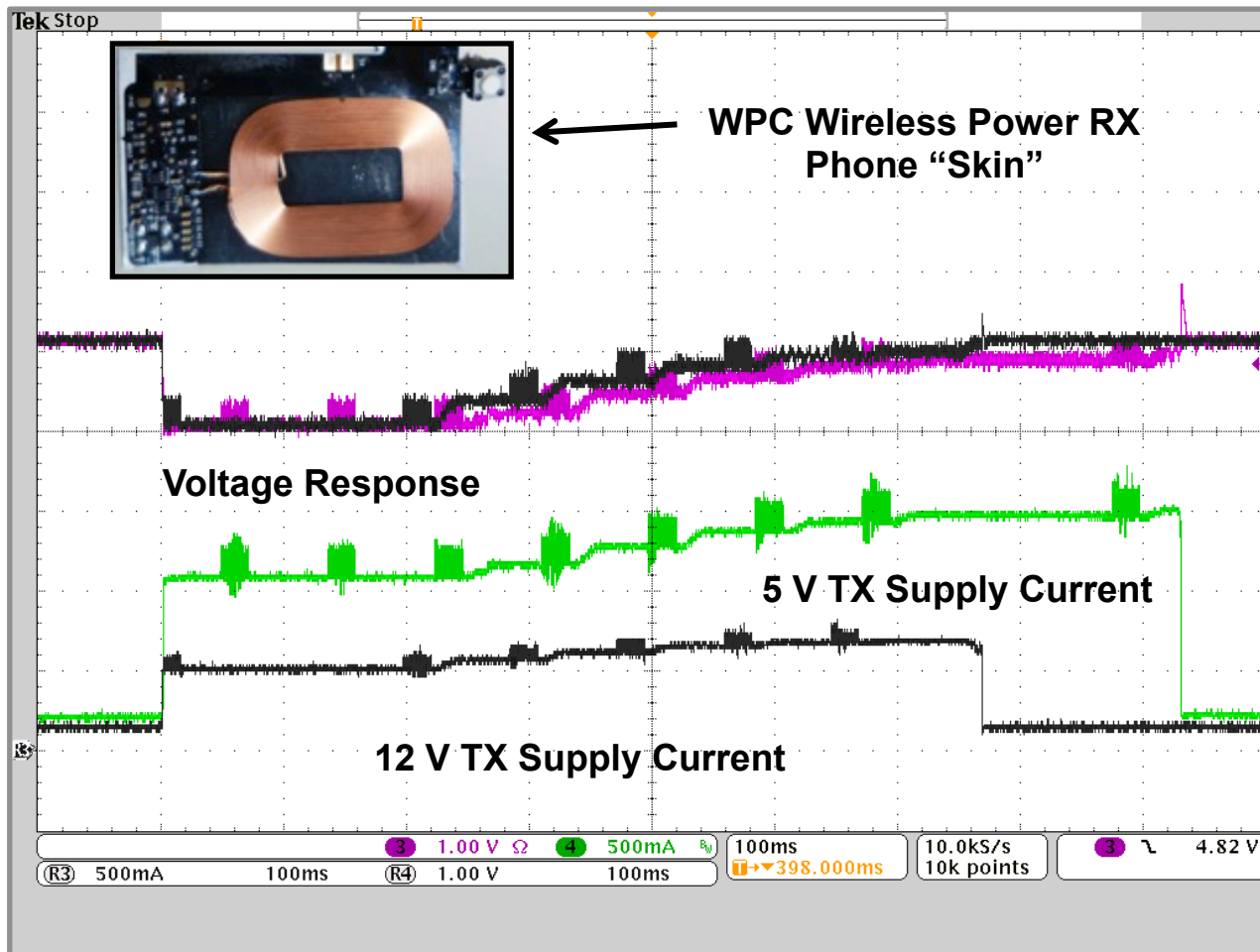
Misaligned coils force  
operation closer to resonance  
 $V_{pp\_tx} = 40 \text{ V}$ ,  $f_{SW} = 135 \text{ kHz}$   
RMS gain = 0.509

# Intelligent Voltage Positioning

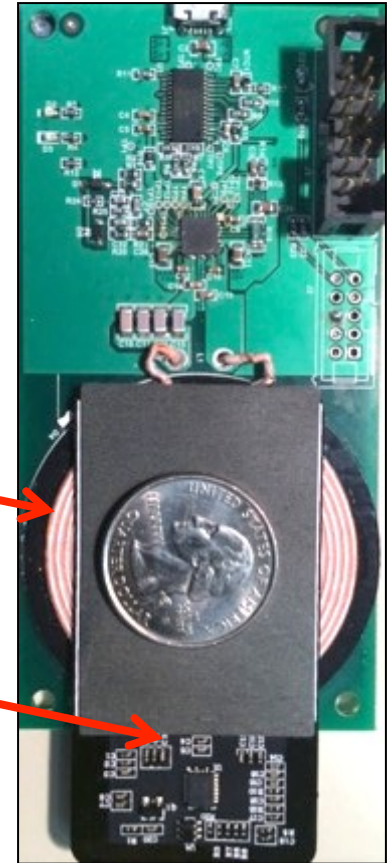
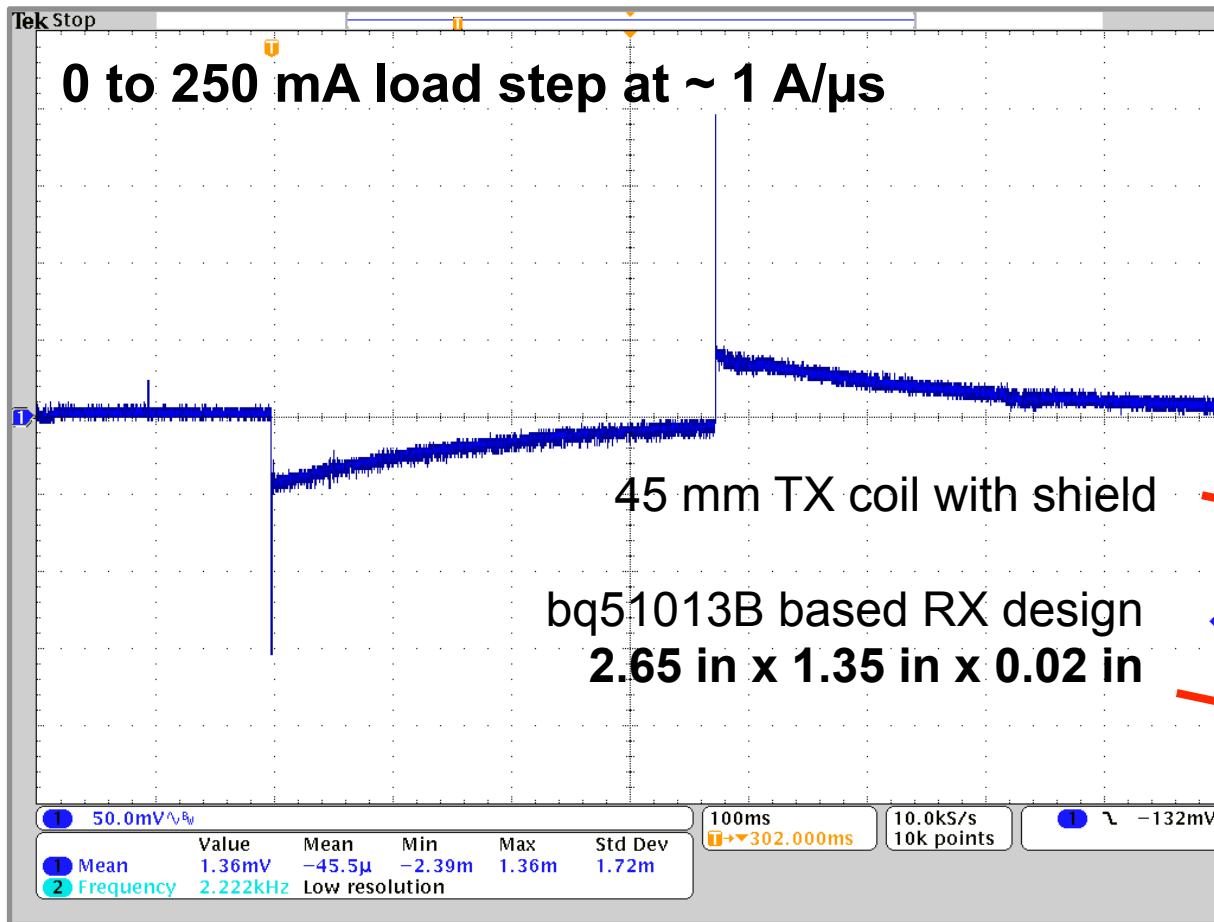


# Transient Load Response

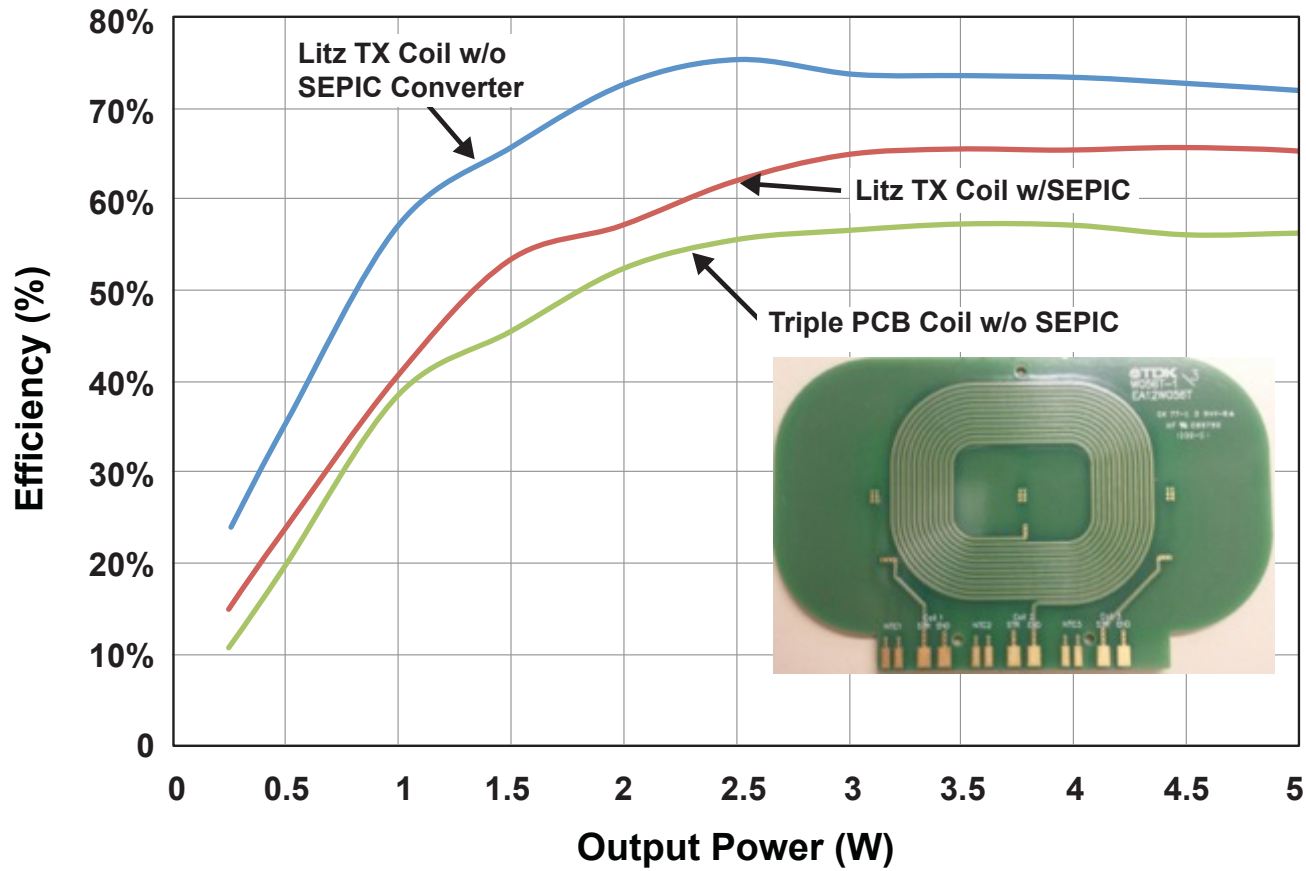
## $I_{OUT} = 0$ to $1$ A



# Transient Load Step Response Litz TX Coil / PCB RX Coil



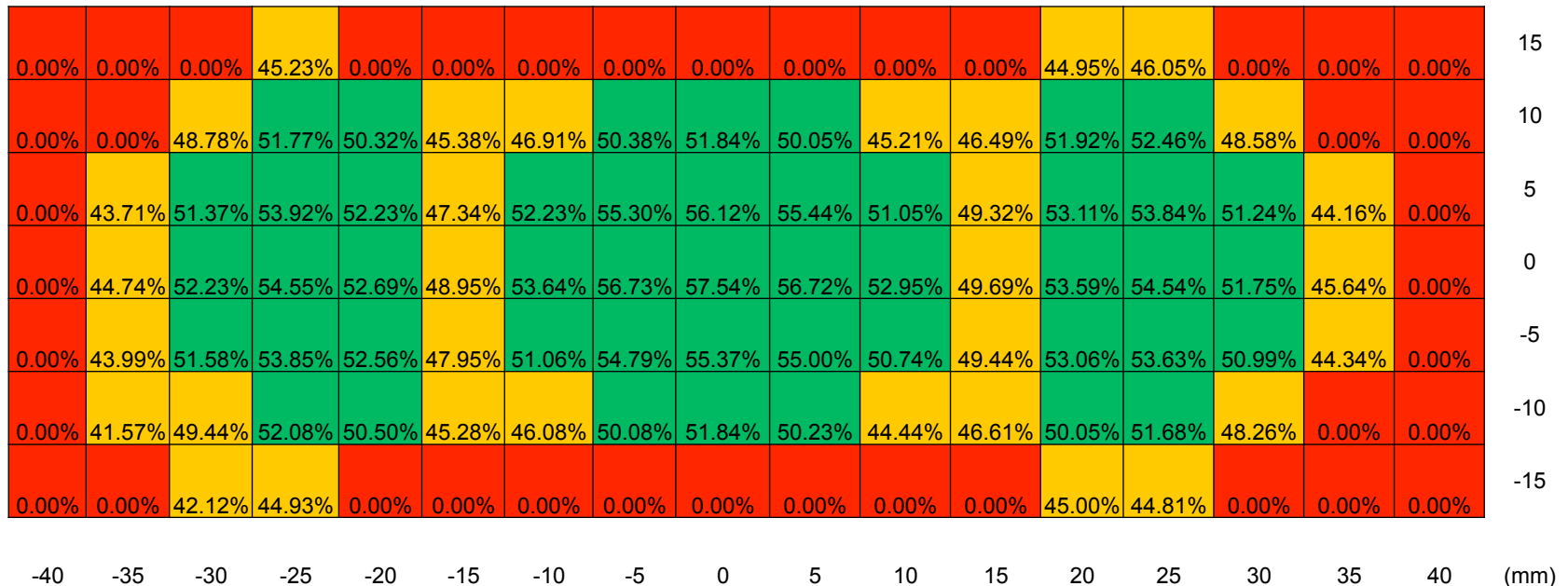
# System Efficiency – DC Input to DC Output PCB Coil vs. 105 Strand Litz Coil



# Designing for Spatial Freedom

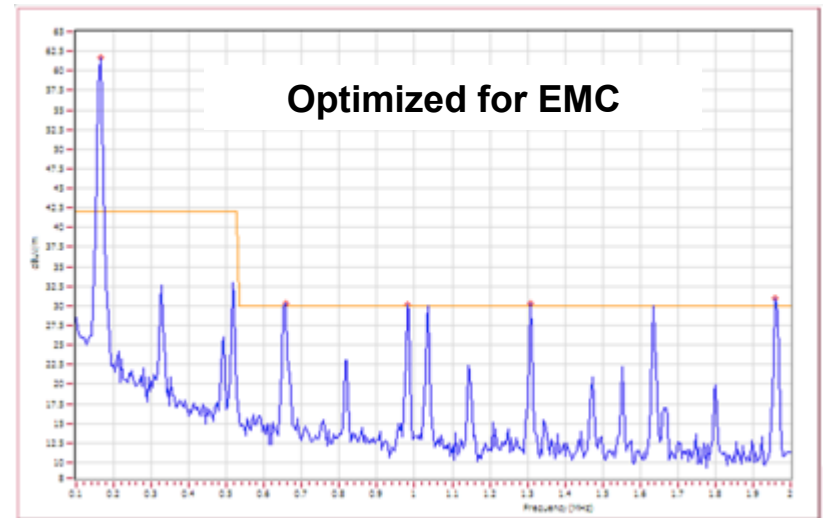
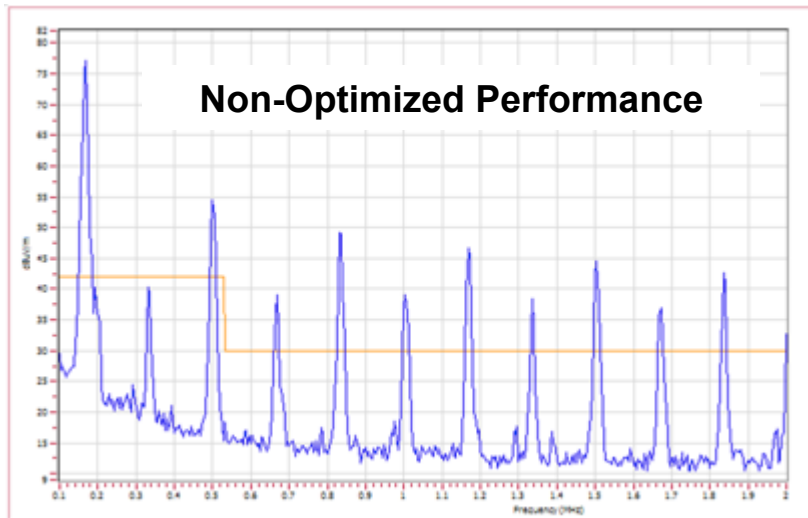
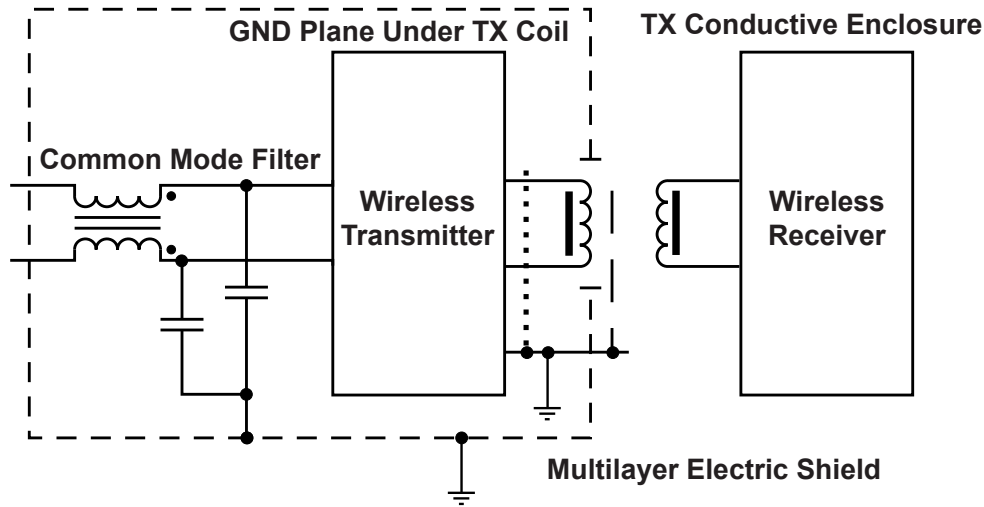
## Efficiency Across Charging Area

- Efficiency map at a 5 W load measured over the PCB coil area
- +/- 40 mm in x-direction and 30 mm in y-direction, 5 mm steps



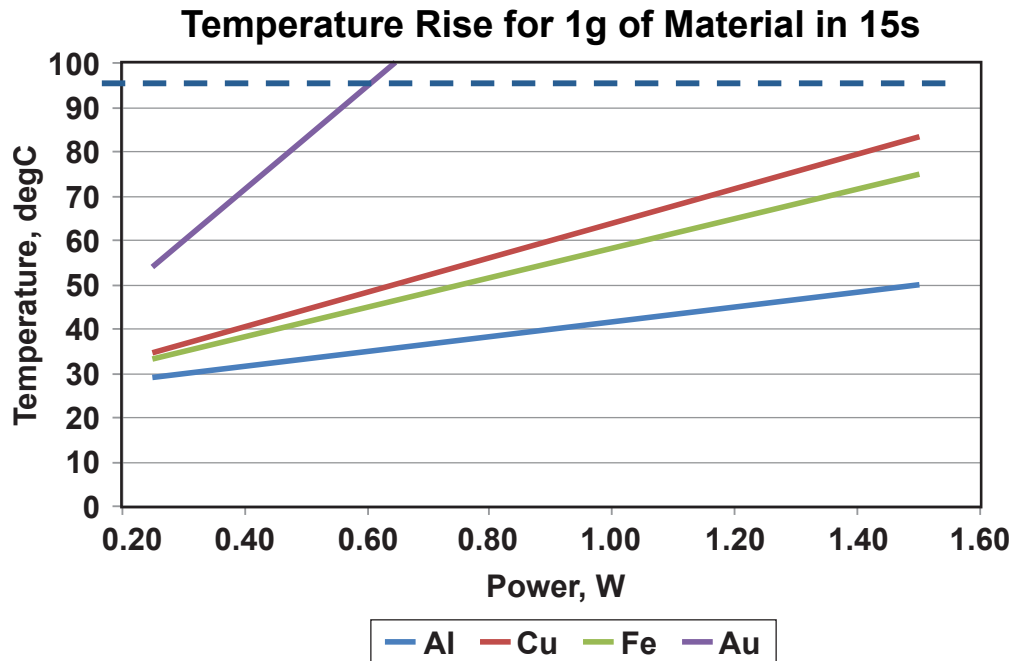


# Design for Electromagnetic Compatibility



# Foreign Object Detection

- Metal objects between TX and RX can induce eddy current losses
- Depending on specific heat capacity, foreign object temp rise can be  $> 60^{\circ}\text{C}$
- Field density of 5 W wireless chargers can result in significant eddy losses
- **Battery pack is especially sensitive**

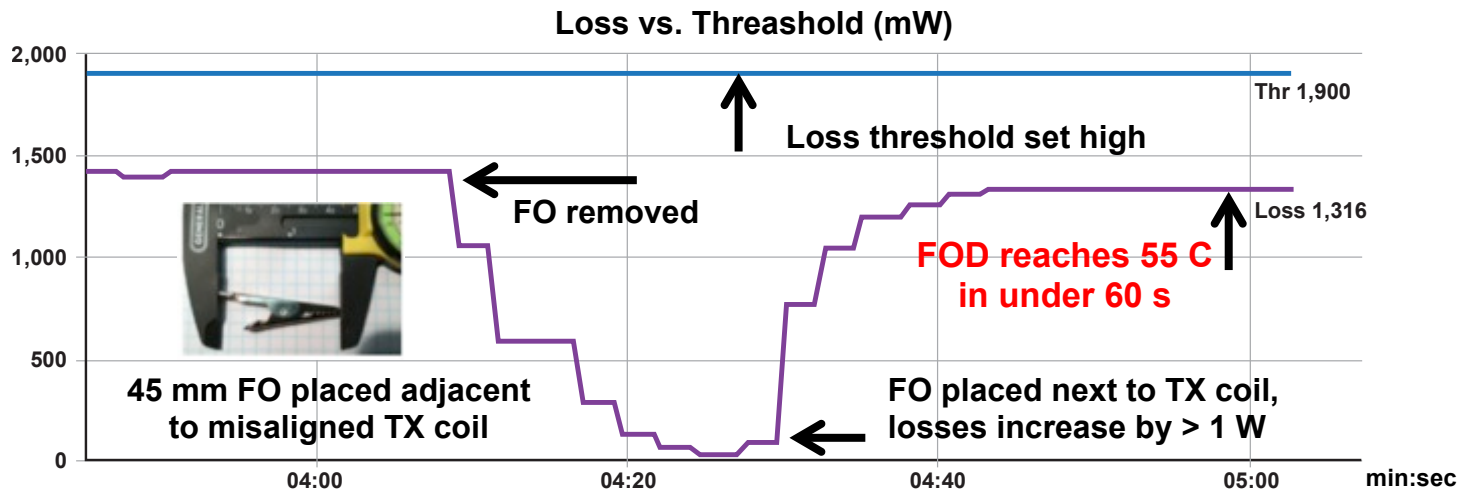
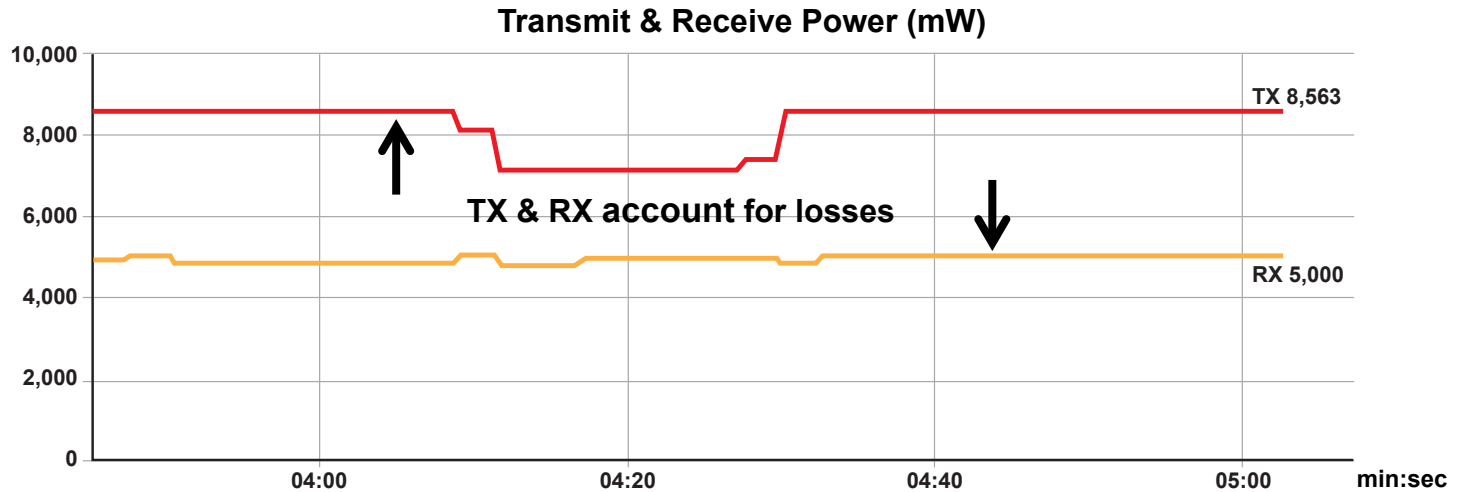


$$\Delta T = \frac{P \times t}{C \times m}$$

Where:

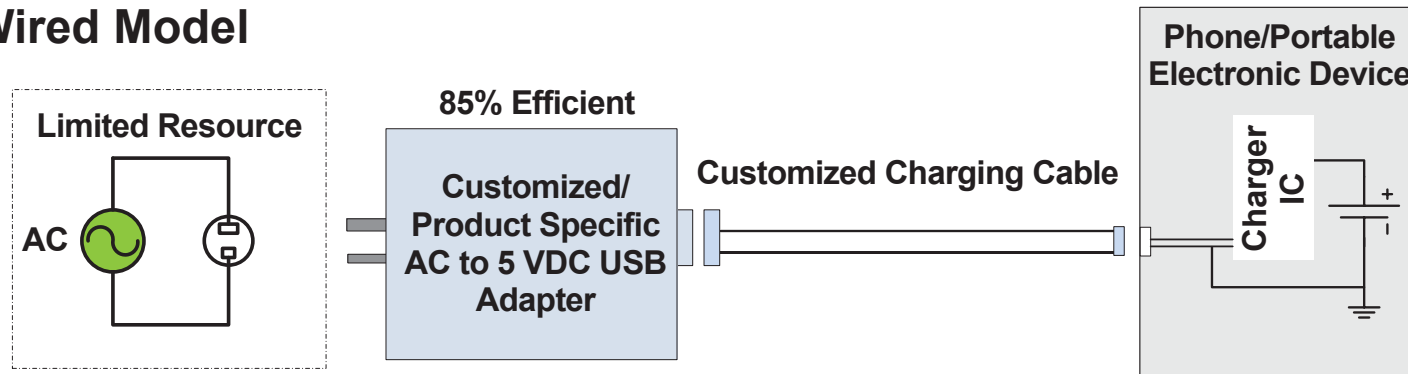
- P = Power dissipated in FO
- C = FO specific heat capacity
- M = FO mass
- t = time

# Dynamic RX / TX Loss Accounting

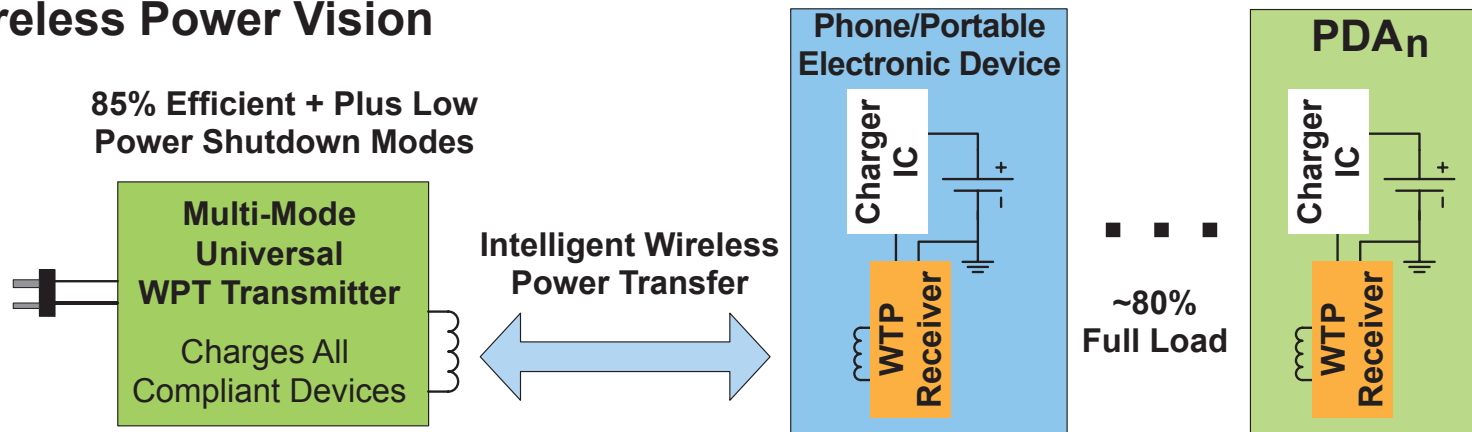


# A Vision for Wireless Power Transfer

## Wired Model



## Wireless Power Vision



# Summary

- Market studies project rapid growth in wireless power technology
- Wireless power transfer is useful when a wired solution is **inconvenient, hazardous or impossible**
- WPT standards have emerged to accelerate growth, reliability, acceptance and safety in consumer electronics
- Developing a wireless power solution does not require compliance to any standard other than those affecting consumer safety and EMC
- Standard compliance may provide advantages in marketability (interoperability), performance, reliability and time to market
- Achieving spatial freedom and good efficiency requires a deep understanding of magnetic field theory

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